Quiz 2

1) Consider 2 individuals who consume two goods: $x$ and $y$. The utility function of individual 1 is

$$
u_{1}\left(x_{1}, y_{1}\right)=\ln \left(x_{1}\right)+y_{1}
$$

and the utility function of individual 2 is

$$
u_{2}\left(x_{2}, y_{2}\right)=\sqrt{x_{2} y_{2}}
$$

The initial endowments of individual 1 is $(2,0)$ which means she has 2 units of $x$ and 0 unit of $y$. The initial endowments of individual 2 is $(1,3)$ which means she has 1 units of $x$ and 3 unit of $y$.
a) Calculate the marginal rate of substitution for both individuals.
b) Show that no-trade (consuming initial endowments) is not Pareto-efficient.
c) Suppose that individual of offers "Give 1 small unit of $y$ and I will give you 1 small amount of $x^{\prime \prime}$. Would they benefit from this trade?
d) Suppose the price of $x$ is $p_{x}$ and the price of $y$ is $p_{y}$. Find the demand for $x$ by individual 1 and individual 2.
e) Compute the competitive equilibrium.
2) Solve the same questions assuming

$$
u_{1}\left(x_{1}, y_{1}\right)=\ln \left(x_{1}\right)+y_{1}
$$

and the utility function of individual 2 is

$$
u_{2}\left(x_{2}, y_{2}\right)=\sqrt{x_{2}}+\sqrt{y_{2}}
$$

