

Kümelerle İlgili Teoremler

$$\begin{aligned}
 A \cup B &= B \cup A \\
 A \cup (B \cup C) &= (A \cup B) \cup C = A \cup B \cup C \\
 A \cap B &= B \cap A \\
 A \cap (B \cap C) &= (A \cap B) \cap C = A \cap B \cap C \\
 A \cap (B \cup C) &= (A \cap B) \cup (A \cap C) \\
 A \cup (B \cap C) &= (A \cup B) \cap (A \cup C) \\
 A \cdot B &= A \cap B' \\
 A \subset B \text{ ise } A' &\supset B' \text{ ya da } B' \subset A' \\
 A \cup \emptyset &= A, A \cap \emptyset = \emptyset \\
 A \cup E &= E, A \cap E = A \\
 (A \cup B)' &= A' \cap B' \\
 (A \cap B)' &= A' \cup B' \\
 A &= (A \cap B) \cup (A \cap B')
 \end{aligned}$$

Permütasyon

$${}_n P_r = \frac{n!}{(n-r)!}$$

Kombinasyon

$$C_{n,r} = {}^n C_r = \frac{n!}{r!(n-r)!}$$

Koşullu Olasılık

$$P(B \setminus A) = \frac{P(A \cap B)}{P(A)}$$

$$P(A_1 \cap A_2 \cap A_3) = P(A_1) P(A_2 | A_1) P(A_3 | A_1 \cap A_2)$$

$$P(A) = P(A_1) P(A | A_1) + P(A_2) P(A | A_2) + \dots + P(A_n) P(A | A_n)$$

Bayes Teoremi

$$P(A_i \setminus E) = \frac{P(A_i) P(E \setminus A_i)}{P(E)}$$

Beklenen Değer

$$E(X) = \sum_{j=1}^n x_j f(x_j)$$

$$E(X) = \int_{-\infty}^{\infty} x f(x) dx$$

Varyans

$$\text{Var}(X) = \sigma_x^2 = \sum_{i=1}^n (x_i - \mu)^2 f(x_i)$$

$$\text{Var}(X) = \sigma_x^2 = \int_{-\infty}^{\infty} (x_i - \mu)^2 f(x) dx$$

$$\text{Var}(X) = \sigma^2 = E[(X - \mu)^2] = E(X^2) - [E(X)]^2$$

Ortak Dağılım

$$E(X) = \mu_X = \sum_x \sum_y x f(x, y)$$

$$E(Y) = \mu_Y = \sum_x \sum_y y f(x, y)$$

$$\sigma_x^2 = E[(X - \mu_X)^2] = \sum_x \sum_y (x - \mu_X)^2 f(x, y)$$

$$\sigma_y^2 = E[(Y - \mu_Y)^2] = \sum_x \sum_y (y - \mu_Y)^2 f(x, y)$$

$$\sigma_{XY} = \sum_x \sum_y (x - \mu_X)(y - \mu_Y) f(x, y)$$

$$\sigma_{XY} = E(XY) - E(X)E(Y) = E(XY) - \mu_X \mu_Y$$

Korelasyon Katsayısı

$$\rho = \frac{\sigma_{XY}}{\sigma_X \sigma_Y}$$

Binom Dağılımı

$$b(x; n, p) = \binom{n}{x} p^x q^{n-x}$$