

Tablo 1 Laplace Dönüşüm Çiftleri

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| | $f(t)$ | $F(s)$ | | $f(t)$ | $F(s)$ |
|----|--|---|----|--|---|
| 1 | $\delta(t)$ | 1 | 2 | $u(t)$ | $\frac{1}{s}$ |
| 3 | t | $\frac{1}{s^2}$ | 4 | $\frac{t^{n-1}}{(n-1)!} \quad (n=1,2,3,\dots)$ | $\frac{1}{s^n}$ |
| 5 | $t^n \quad (n=1,2,3,\dots)$ | $\frac{n!}{s^{n+1}}$ | 6 | e^{-at} | $\frac{1}{s+a}$ |
| 7 | $t \cdot e^{-at}$ | $\frac{1}{(s+a)^2}$ | 8 | $\frac{1}{(n-1)!} t^{n-1} e^{-at} \quad (n=1,2,3,\dots)$ | $\frac{1}{(s+a)^n}$ |
| 9 | $t^n \cdot e^{-at} \quad (n=1,2,3,\dots)$ | $\frac{n!}{(s+a)^{n+1}}$ | 10 | $\sin \omega t$ | $\frac{\omega}{s^2 + \omega^2}$ |
| 11 | $\cos \omega t$ | $\frac{s}{s^2 + \omega^2}$ | 12 | $\sinh \omega t$ | $\frac{\omega}{s^2 - \omega^2}$ |
| 13 | $\cosh \omega t$ | $\frac{s}{s^2 - \omega^2}$ | 14 | $\frac{1}{a}(1 - e^{-at})$ | $\frac{1}{s(s+a)}$ |
| 15 | $\frac{1}{b-a}(e^{-at} - e^{-bt})$ | $\frac{1}{(s+a)(s+b)}$ | 16 | $\frac{1}{b-a}(be^{-bt} - ae^{-at})$ | $\frac{s}{(s+a)(s+b)}$ |
| 17 | $\frac{1}{ab} \left[1 + \frac{1}{a-b} (be^{-at} - ae^{-bt}) \right]$ | $\frac{1}{s(s+a)(s+b)}$ | 18 | $\frac{1}{a^2}(1 - e^{-at} - ate^{-at})$ | $\frac{1}{s(s+a)^2}$ |
| 19 | $\frac{1}{a^2}(at - 1 + e^{-at})$ | $\frac{1}{s^2(s+a)}$ | 20 | $e^{-at} \sin \omega t$ | $\frac{\omega}{(s+a)^2 + \omega^2}$ |
| 21 | $e^{-at} \cos \omega t$ | $\frac{s+a}{(s+a)^2 + \omega^2}$ | 22 | $\frac{\omega_n}{\sqrt{1-\zeta^2}} e^{-\zeta \omega_n t} \sin \omega_n \sqrt{1-\zeta^2} t$ | $\frac{\omega_n^2}{s^2 + 2\zeta \omega_n s + \omega_n^2}$ |
| 23 | $-\frac{1}{\sqrt{1-\zeta^2}} e^{-\zeta \omega_n t} \sin(\omega_n \sqrt{1-\zeta^2} t - \phi), \phi = \tan^{-1} \frac{\sqrt{1-\zeta^2}}{\zeta}$ | | | $\frac{s}{s^2 + 2\zeta \omega_n s + \omega_n^2}$ | |
| 24 | $1 - \frac{1}{\sqrt{1-\zeta^2}} e^{-\zeta \omega_n t} \sin(\omega_n \sqrt{1-\zeta^2} t + \phi), \phi = \tan^{-1} \frac{\sqrt{1-\zeta^2}}{\zeta}$ | | | $\frac{\omega_n^2}{s(s^2 + 2\zeta \omega_n s + \omega_n^2)}$ | |
| 25 | $1 - \cos \omega t$ | $\frac{\omega^2}{s(s^2 + \omega^2)}$ | 26 | $\omega t - \sin \omega t$ | $\frac{\omega^3}{s^2(s^2 + \omega^2)}$ |
| 27 | $\sin \omega t - \omega t \cos \omega t$ | $\frac{2\omega^3}{(s^2 + \omega^2)^2}$ | 28 | $\frac{1}{2\omega} t \sin \omega t$ | $\frac{s}{(s^2 + \omega^2)^2}$ |
| 29 | $t \cos \omega t$ | $\frac{s^2 - \omega^2}{(s^2 + \omega^2)^2}$ | 30 | $\frac{1}{2\omega} (\sin \omega t + \omega t \cos \omega t)$ | $\frac{s^2}{(s^2 + \omega^2)^2}$ |
| 31 | $\frac{1}{\omega_2^2 - \omega_1^2} (\cos \omega_1 t - \cos \omega_2 t) \quad (\omega_1^2 \neq \omega_2^2)$ | | | $\frac{s}{(s^2 + \omega_1^2)(s^2 + \omega_2^2)}$ | |
| 32 | $\frac{1}{\omega} \sqrt{(\alpha - a) + \omega} \cdot e^{-at} \sin(\omega t + \phi), \phi = \tan^{-1} \frac{\omega}{\alpha - a}$ | | | $\frac{s + \alpha}{(s+a)^2 + \omega^2}$ | |

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|-----------|--|-----------|--|
| 1 | $\mathcal{L}[Af(t)] = AF(s)$ | 2 | $\mathcal{L}[f_1(t) \pm f_2(t)] = F_1(s) \pm F_2(s)$ |
| 3 | $\mathcal{L}_{\pm} \left[\frac{d}{dt} f(t) \right] = sF(s) - f(0\pm)$ | 4 | $\mathcal{L}_{\pm} \left[\frac{d^2}{dt^2} f(t) \right] = s^2 F(s) - sf(0\pm) - \dot{f}(0\pm)$ |
| 5 | $\mathcal{L}_{\pm} \left[\frac{d^n}{dt^n} f(t) \right] = s^n F(s) - \sum_{k=1}^n s^{n-k} f^{(k-1)}(0\pm), \quad f^{(k-1)}(t) = \frac{d^{k-1}}{dt^{k-1}} f(t)$ | | |
| 6 | $\mathcal{L}_{\pm} \left[\int f(t) dt \right] = \frac{F(s)}{s} + \frac{\left[\int f(t) dt \right]_{t=0\pm}}{s}$ | 7 | $\mathcal{L}_{\pm} \left[\int_0^t f(t) dt \right] = \frac{F(s)}{s}$ |
| 8 | $\mathcal{L}_{\pm} \left[\int \int f(t) dt dt \right] = \frac{F(s)}{s^2} + \frac{\left[\int f(t) dt \right]_{t=0\pm}}{s^2} + \frac{\left[\int \int f(t) dt dt \right]_{t=0\pm}}{s}$ | | |
| 9 | $\mathcal{L}_{\pm} \left[\int \dots \int f(t) (dt)^n \right] = \frac{F(s)}{s^n} + \sum_{k=1}^n \frac{1}{s^{n-k+1}} \left[\dots \int f(t) (dt)^k \right]_{t=0\pm}$ | | |
| 10 | $\int_0^{\infty} f(t) dt = \lim_{s \rightarrow 0} F(s), \quad \int_0^{\infty} f(t) dt \text{ varsa}$ | 11 | $\mathcal{L} \left[e^{-at} f(t) \right] = F(s+a)$ |
| 12 | $\mathcal{L} \left[f(t-\alpha) I(t-\alpha) \right] = e^{-as} F(s) \quad \alpha \geq 0$ | 13 | $\mathcal{L} \left[t f(t) \right] = -\frac{dF(s)}{ds}$ |
| 14 | $\mathcal{L} \left[t^2 f(t) \right] = \frac{d^2}{ds^2} F(s)$ | 15 | $\mathcal{L} \left[t^n f(t) \right] = (-1)^n \frac{d^n}{ds^n} F(s) \quad n=1,2,3,\dots$ |
| 16 | $\mathcal{L} \left[\frac{1}{t} f(t) \right] = \int_s^{\infty} F(s) ds$ | 17 | $\mathcal{L} \left[f \left(\frac{t}{a} \right) \right] = aF(as)$ |