



Yildiz Technical University  
Faculty of Civil Engineering  
Department of Geomatic Engineering



# TOPOGRAPHY (HRT3351)

Lecture Notes

Prof. Dr. Burak AKPINAR

Title	Code	Local Credit	ECTS	Lecture (hour/week)	Practical (hour/week)	Laboratory (hour/week)
Topography	HRT3351	3	4	3	0	0

### Course Objectives

The aim of this course, gains required skills of basic of surveying techniques, mathematical definitions using for large scale map production.

**Prof. Dr. Burak AKPINAR**

<http://www.avesis.yildiz.edu.tr/bakpinar>  
[bakpinar@yildiz.edu.tr](mailto:bakpinar@yildiz.edu.tr)

# WEEKLY SUBJECTS

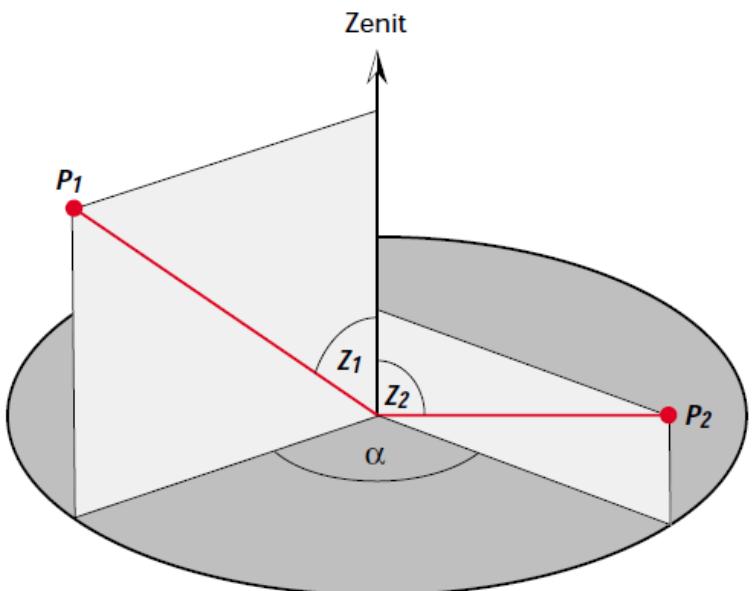
Week	Subject
1	Introduction to Topography
2	Measurement Units and Sources of Measurement Errors
3	Types of Errors
4	Coordinate Systems and Map Projections
5	Geodetic Network Points and Distance Measurements
6	Direction Measurements
7	Traverse Computations
8	Height Measurements
9	Midterm exam 1
10	Area and Volume Computations
11	Field work
12	Field work
13	Geographic Information System, GIS
14	Midterm exam 2
15	GNSS Global Positioning Systems
16	Final exam

# **Week-6**

## **Direction Measurements and Geodetic Fundamental Computations**

# Direction and Angle

An angle is defined as the difference in direction between two convergent lines.



$$\alpha = r_2 - r_1$$

$Z_1, Z_2 \rightarrow$  Vertical Angle

# Angle Measurement Equipments



Mechanical Theodolite



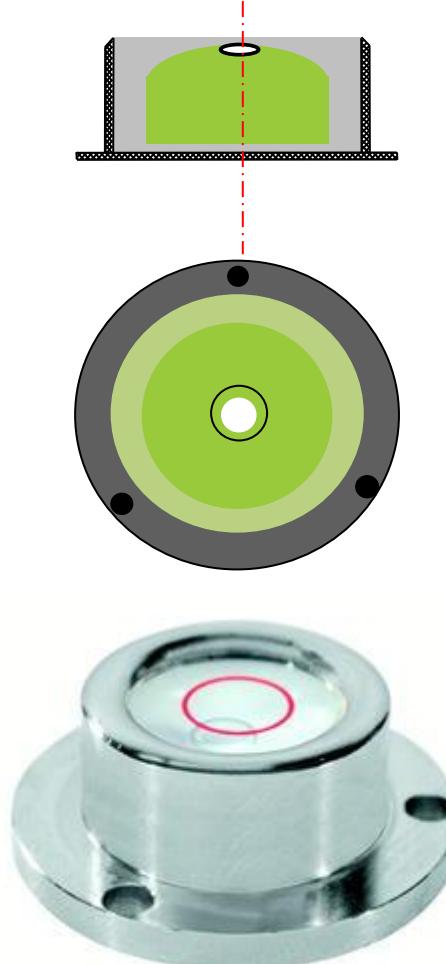
Electronic Theodolite



Total Station

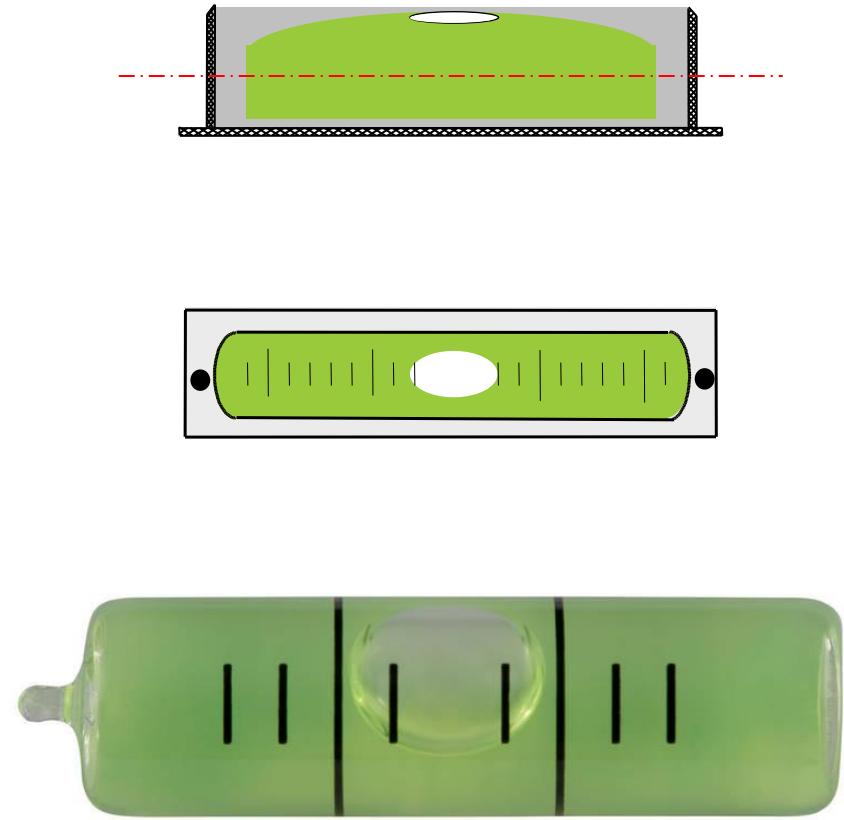
# Angle Measurement Equipments

Circular Level



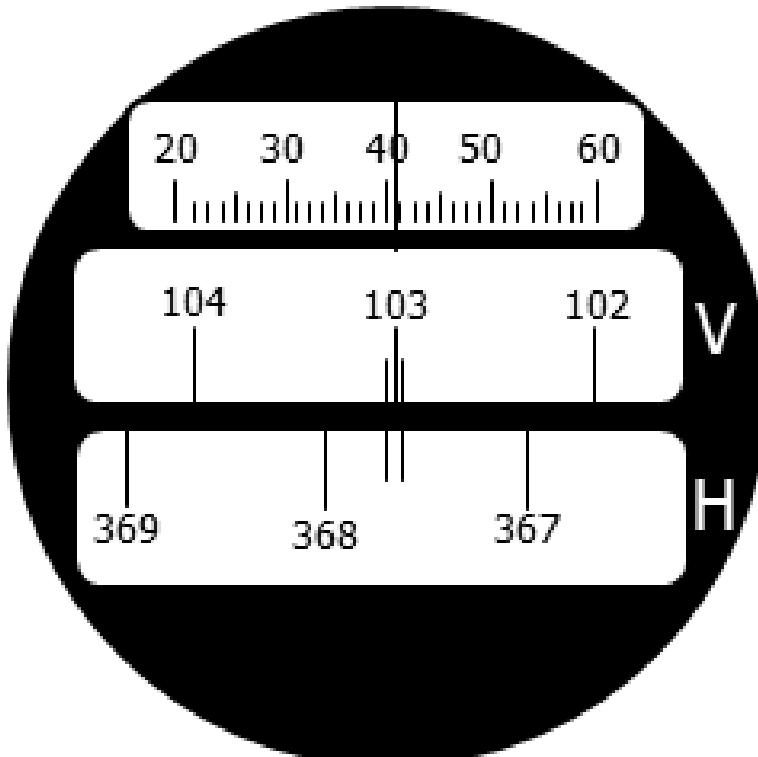
Precision : 5 '-10'

Cylindrical Level

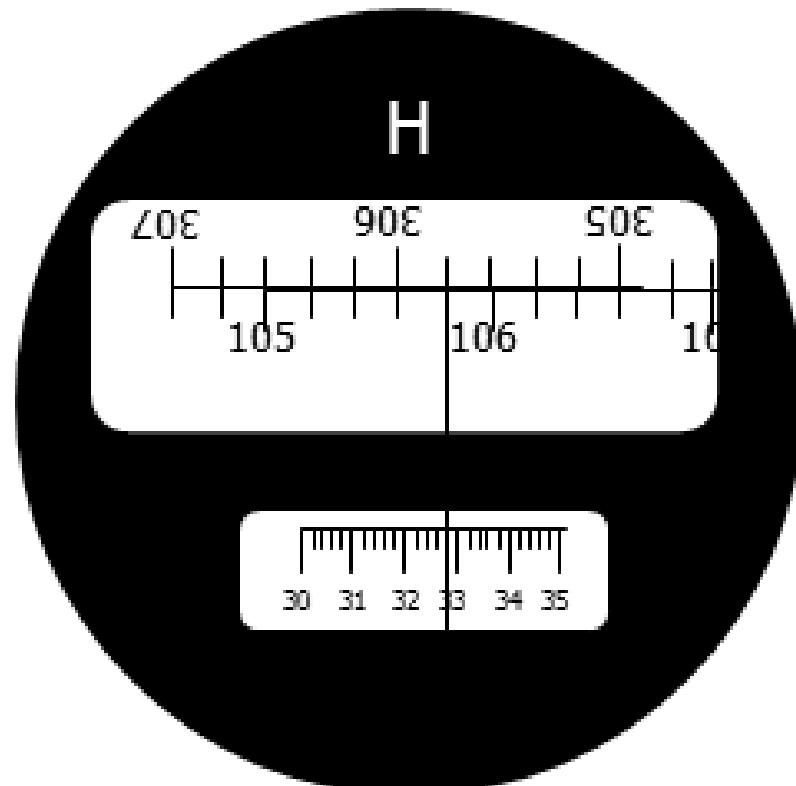


Precision : 10 " - 30"

# Direction Measurement

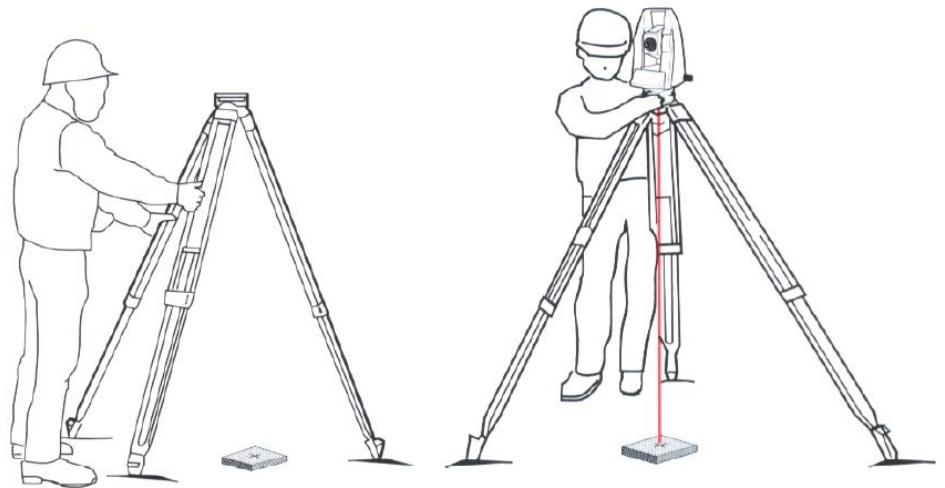


V: 103.405 gon

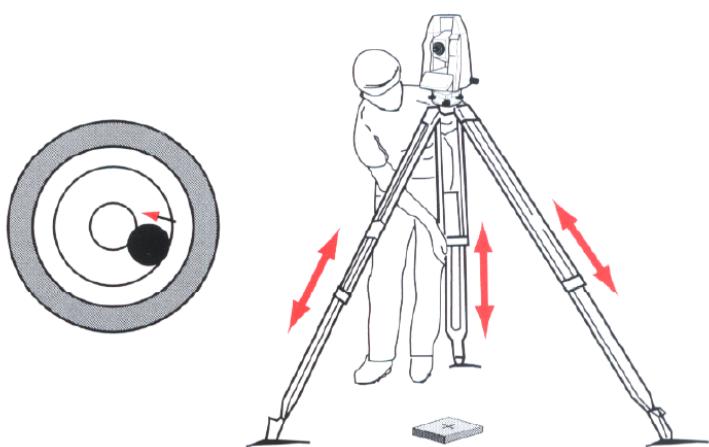


H: 105.8328 gon

## 1. Centering

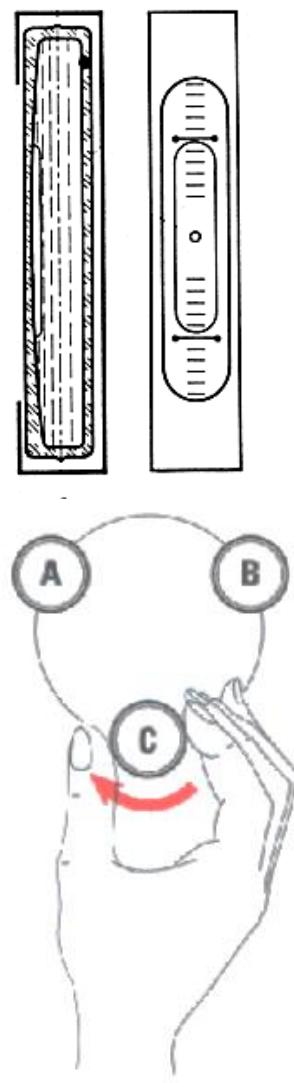
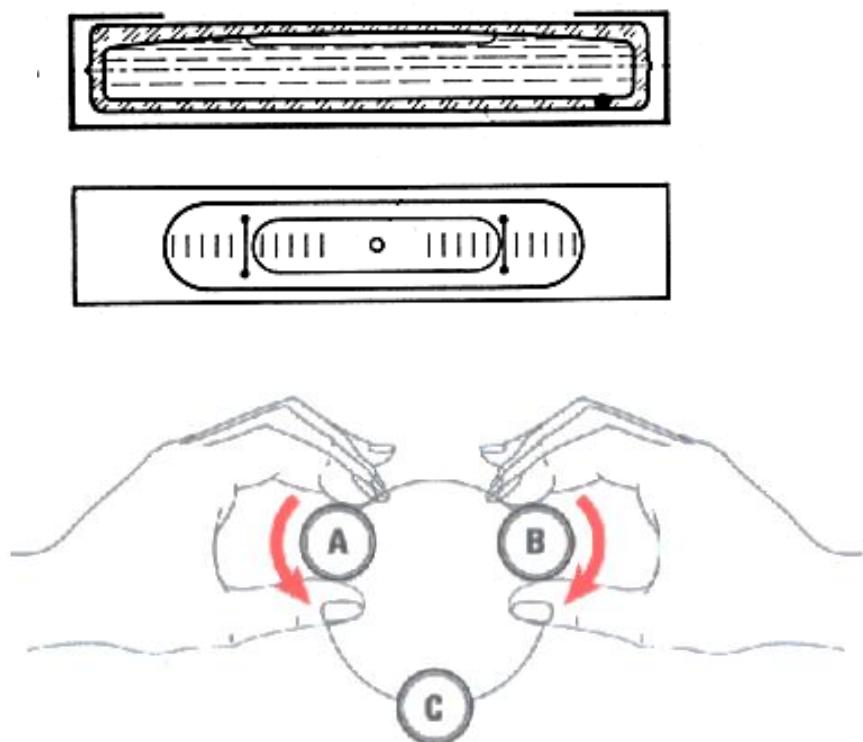


## 2. Circular Level

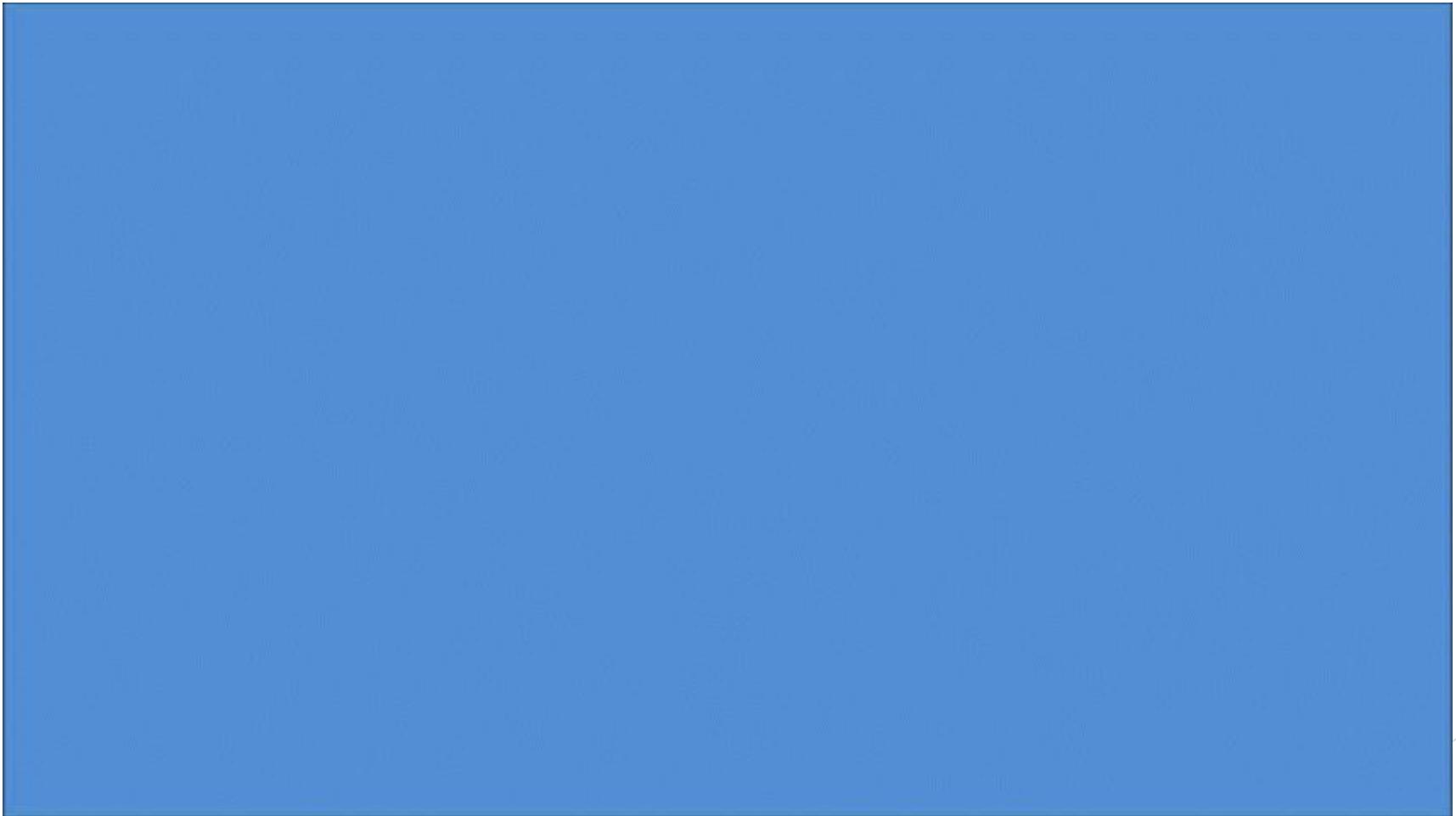


# Setting up the Theodolite

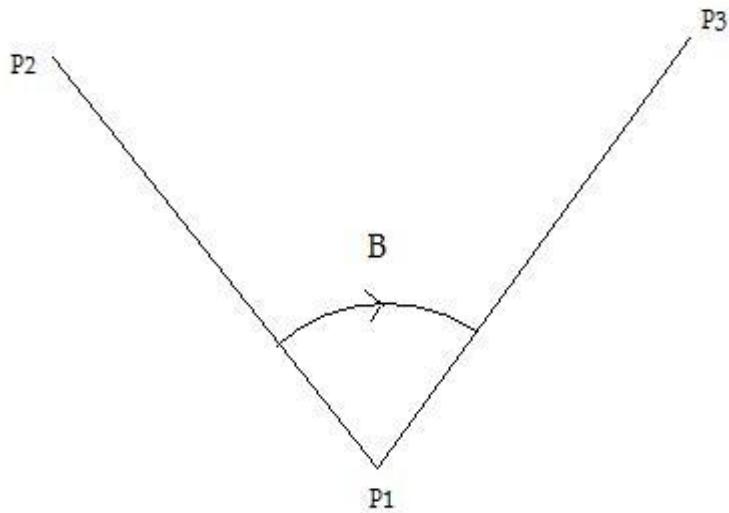
## 3. Cylindrical Level



# Setting up the Theodolite



# Horizontal Angle Measurement



$P_2$  – left target (back sight)

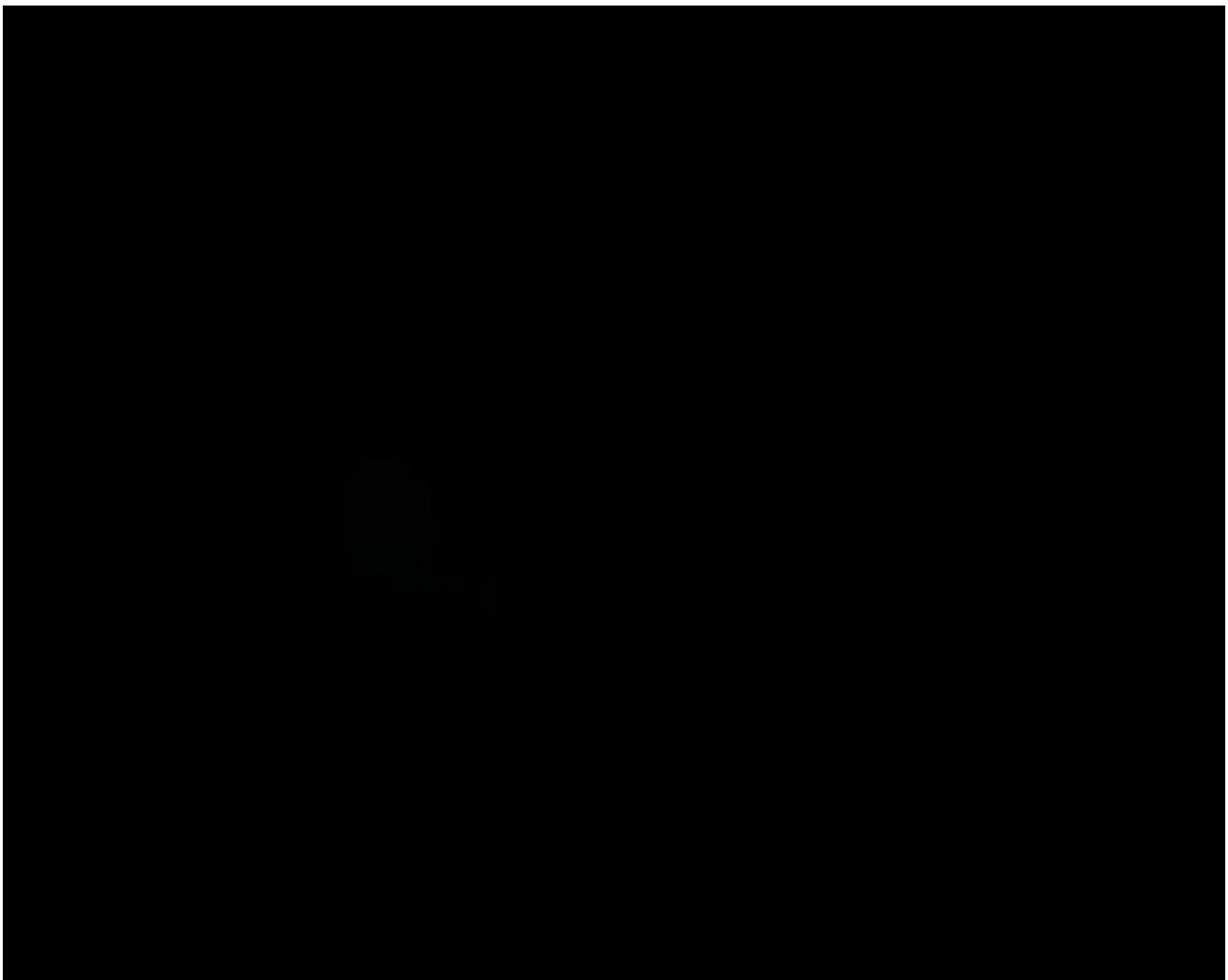
$P_3$  – right target (foresight)

$B$  : horizontal angle (clockwise)

Face I =  $P_2$  then  $P_3$  observations

Face II =  $P_3$  then  $P_2$  observations

# Horizontal Angle Measurement



# Horizontal Angle Measurement

FIELD BOOK FOR ANGULAR MEASUREMENTS - HORIZONTAL ANGLE						
	Station	Target	Horizontal Direction (GRAD)		Mean	Reduced
	Point	Point	Face I	Face II	$(F_{II} - 200 + F_I)/2$	directions(GRAD) (GRAD)
SET1	P <sub>2</sub>	P <sub>1</sub>	0.650	200.652	0.651	0.0000
		P <sub>3</sub>	149.298	349.296	149.297	148.646
SET2	P <sub>2</sub>	P <sub>1</sub>	100.323	300.325	100.324	0.0000
		P <sub>3</sub>	248.971	48.973	248.972	148.648
PROJECT:			GROUP NO:			
LOCATION:			BOOKER:			
WEATHER:			OPERATOR:			
EQUIPMENT:			DATE:			

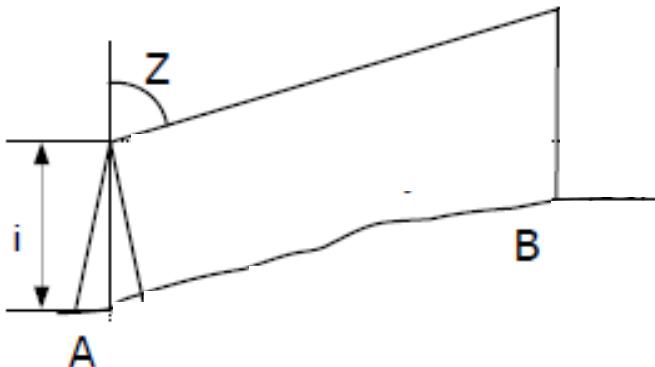
# Horizontal Angle Measurement

DN	BN	Directions		Reduction to 0		Mean	Final Directions	d (cc)	v (cc)	w (cc)
		1. Durum	2. Durum	1. Durum	2. Durum			(cc)	(cc)	(cc)
P <sub>1</sub>	P <sub>2</sub>	0° 00' 45	200° 00' 48	0° 00' 00	0° 00' 00	0° 00' 00	0° 00' 00	0	1.7	2.89
	P <sub>3</sub>	11.28 34	211.28 46	11.27 89	11.27 98	11.27 94	11.27 90	-4	-2.3	5.29
	P <sub>4</sub>	226.36 64	26.36 84	226.36 19	226.36 36	226.36 27	226.36 26	-1	0.7	0.49
		(0.00 56)	200.00 65)					-5		
							5/ 3 =	-1.7		
P <sub>1</sub>	P <sub>2</sub>	100.00 43	300.00 45	0.00 00	0.00 00	0.00 00		0	-1.7	2.89
	P <sub>3</sub>	111.28 31	311.28 29	11.27 88	11.27 84	11.27 86		4	2.3	5.29
	P <sub>4</sub>	326.36 68	126.36 71	226.36 25	226.36 26	226.36 25		1	-0.7	0.49
		(100.00 49)	300.00 54)					5		17.34
							5/ 3 =	1.7		

$$m = \pm \sqrt{\frac{[wv]}{(n-1)(s-1)}} = \pm \sqrt{\frac{17.34}{(2-1)(3-1)}} = \pm \sqrt{\frac{17.34}{2}} = \pm 2^{\circ}.94$$

$$M = \pm \frac{m}{\sqrt{n}} = \pm \frac{2.94}{\sqrt{2}} = \pm 2^{\circ}.08$$

# Vertical Angle Measurement



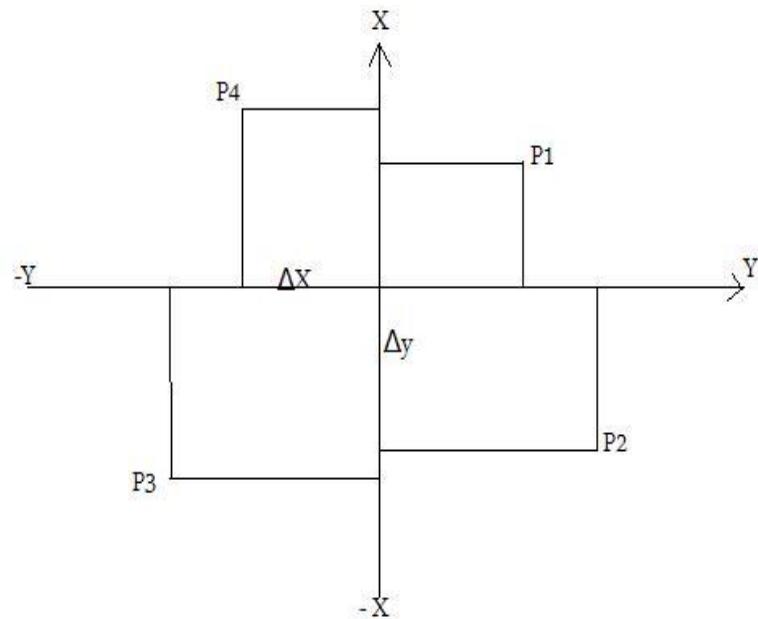
DN	BN	Set	Face	Vertical Angle (Z)	$\bar{\delta}$	Corrected Angle (Z)	Mean of Set(Z)	$v_{\delta}$	$V_{\delta}^2$
A	B	1	I	95°.7718	-30°°	95°.7688	95°.7689	-3	9
			II	304.2342	-30°°	304.2312			
				400.0060		400.0000			
	C	2	I	95.7730	-40°°	95.7690		+7	49
			II	304.2350	-40°°	304.2310			
				400.0080		400.0000			
C	1	I	I	107.3641	-35°°	107.3606	107.3601	+2	4
			II	292.6429	-35°°	292.6394			
				400.0070		400.0000			
	2	I	I	107.3623	-27°°	107.3596		-6	36
			II	292.6431	-27°°	292.6404			
				400.0054	$\bar{\delta}_{\text{ort}} = -33$	400.0000			

# Geodetic Fundamental Computations

TOPOGRAPHY (HRT3351)

Prof. Dr. Burak AKPINAR

# Rectangular Coordinate System

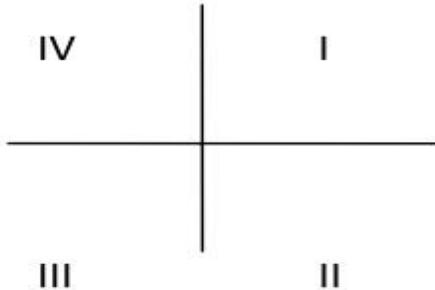


In plane surveys it is convenient to perform the work in a rectangular  $XY$  coordinate system.

Direction of  $+X$  refers to north,

Direction of  $+Y$  refers to east,

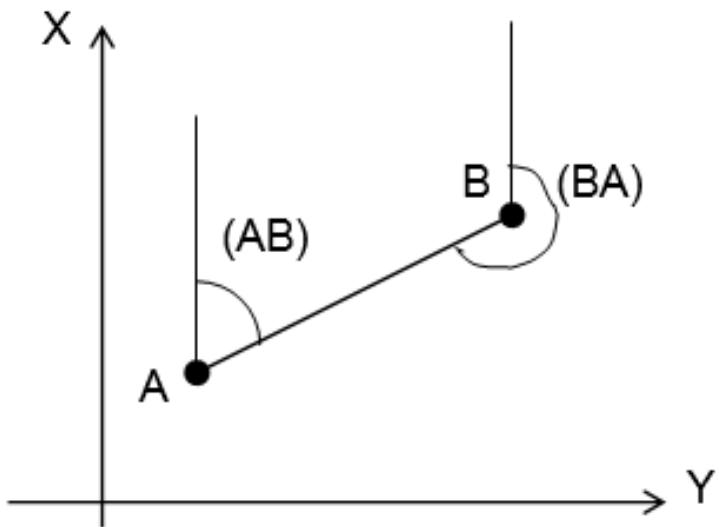
# Rectangular Coordinate System



The  $x$  and  $y$  axes divide the plane into four parts. The quadrants are numbered clockwise starting with the upper right quadrant.

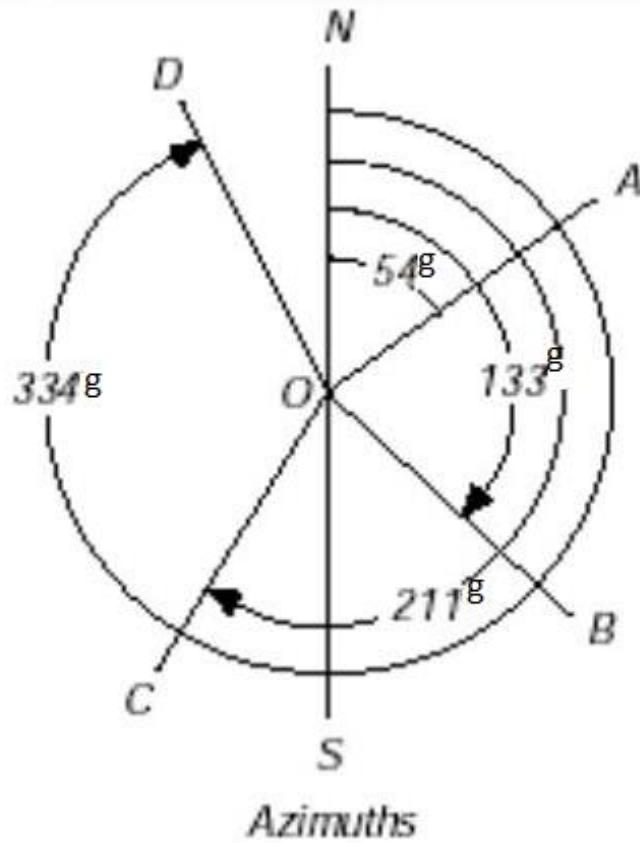
QUADRANT	$\Delta X$	$\Delta Y$
I. QUADRANT	+	+
II. QUADRANT	-	+
III. QUADRANT	-	-
IV. QUADRANT	+	-

# Azimuth



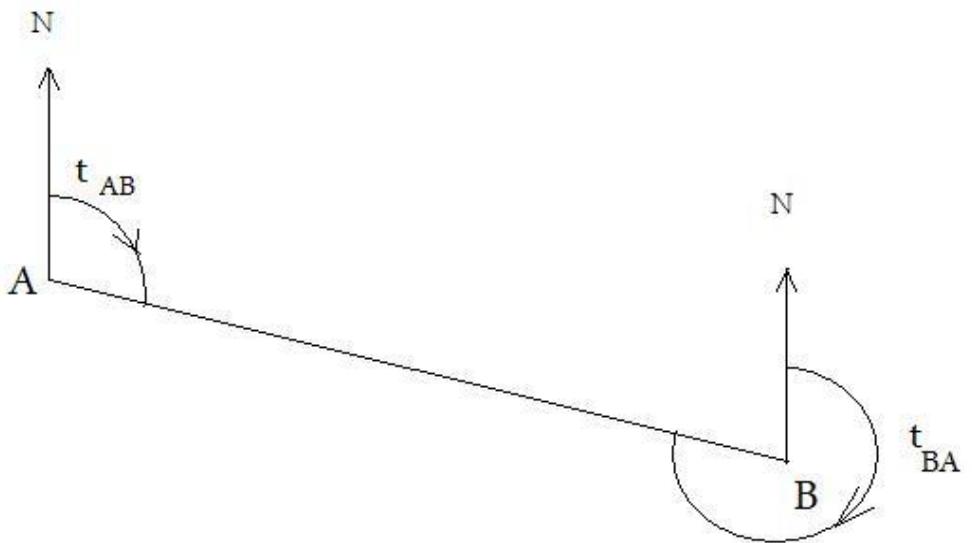
- The azimuth of a line on the ground is its horizontal angle measured clockwise from the meridian to the line.
- Azimuth gives the direction of the line with respect to the meridian.
- In plan surveying azimuths are generally measured from the north.
- Azimuths may have values between  $0^{\circ}$  and  $400^{\circ}$  ( $0 - 360$  degrees).

# Azimuth



Line	Azimuth
O - A	$54^{\circ}$
O - B	$133^{\circ}$
O - C	$211^{\circ}$
O - D	$334^{\circ}$

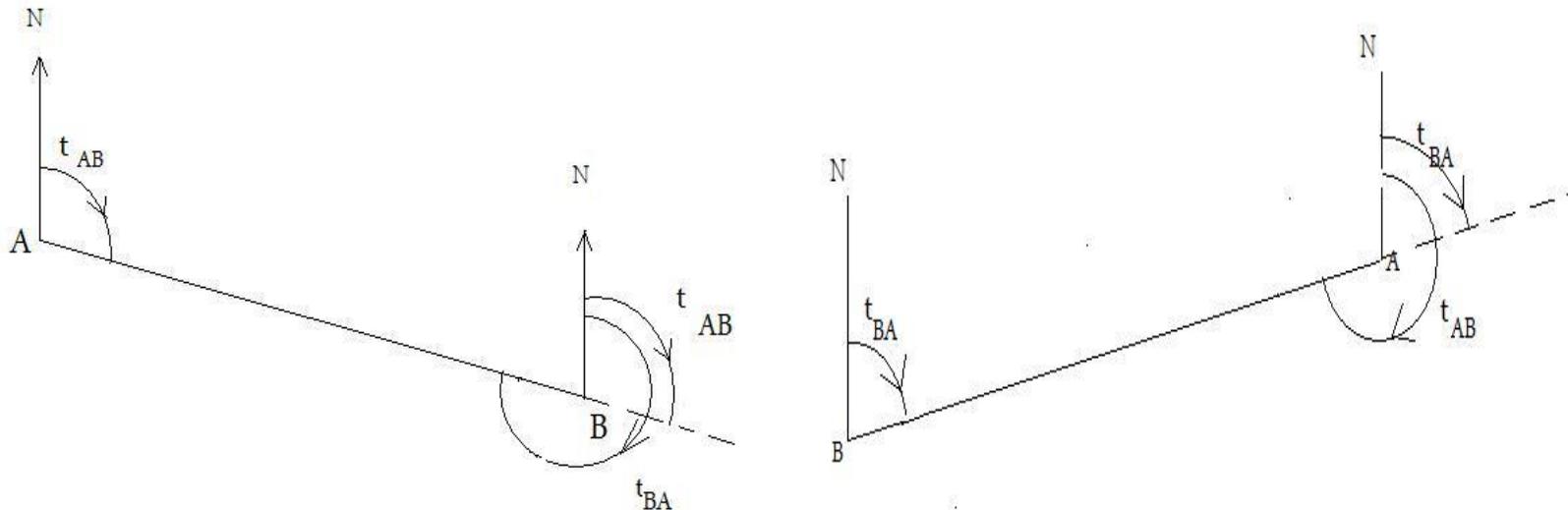
# Azimuth



$t_{AB}$  = forward azimuth of AB line

$t_{BA}$  = back azimuth of AB line

# Azimuth

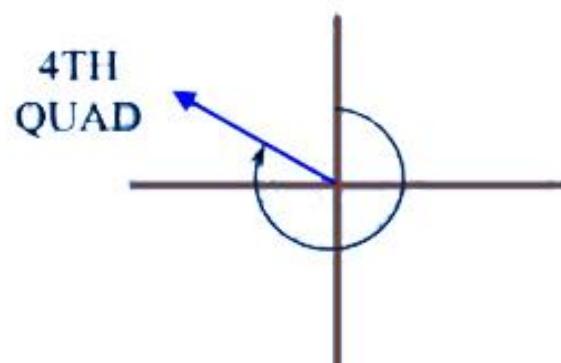
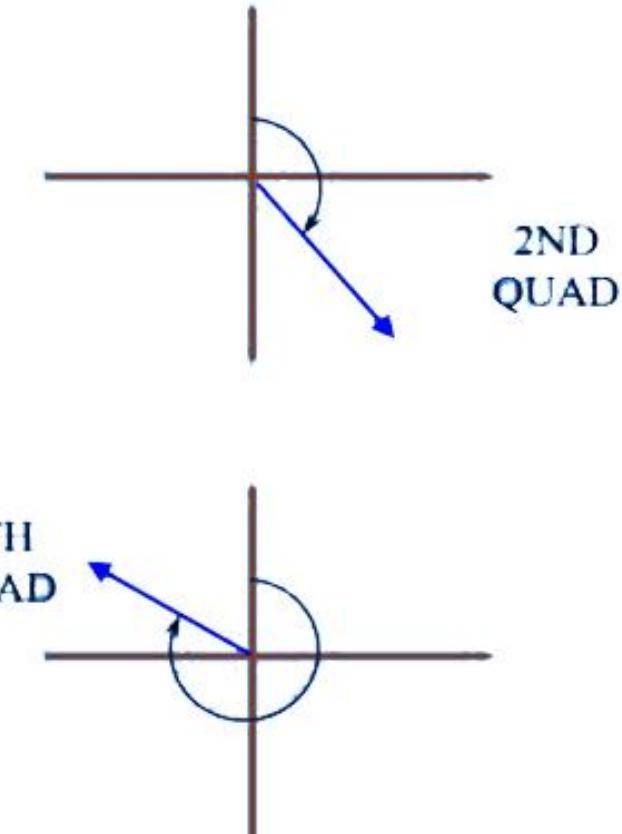
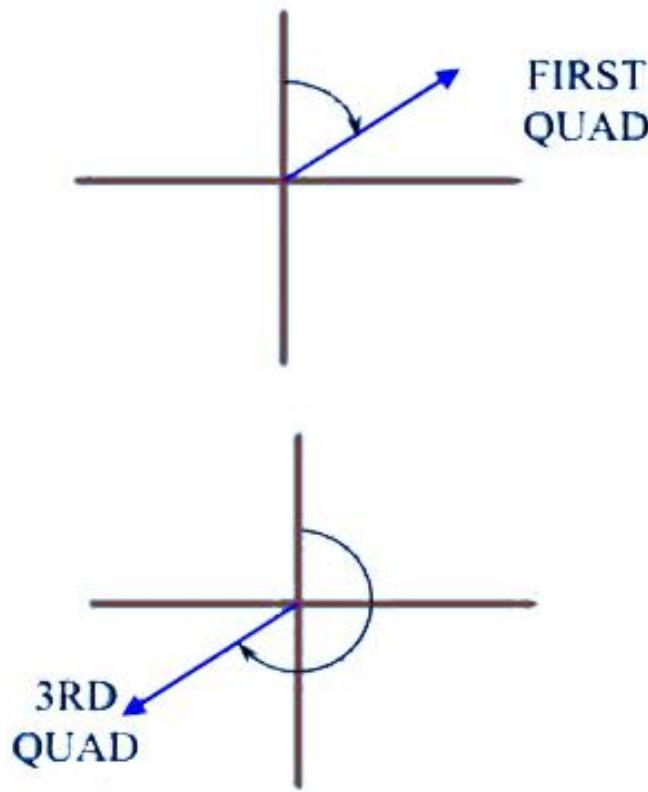


In plane surveying, forward azimuths are converted to back azimuths, and vice versa, by adding or subtracting  $200^g$ .

$$t_{AB} < 200^g \rightarrow t_{BA} = t_{AB} + 200^g$$

$$t_{AB} > 200^g \rightarrow t_{BA} = t_{AB} - 200^g$$

# Rectangular Coordinate System



# Fundamental Computation - 1

Known: A ( $X_A, Y_A$ )

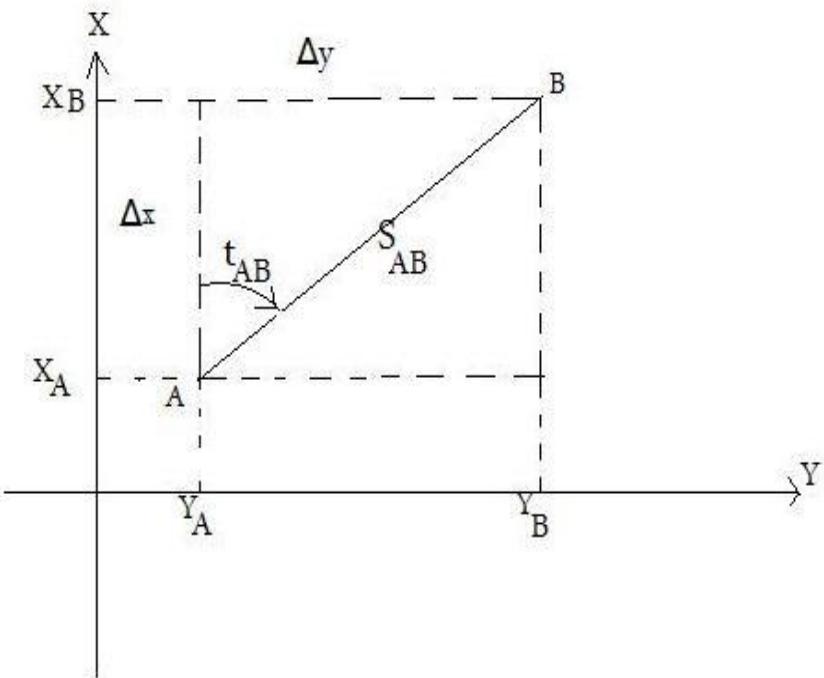
$S_{AB}$

$t_{AB} = \alpha$

Unknown: B ( $X_B, Y_B$ )

$$\sin \alpha = \frac{\Delta Y}{S} \rightarrow \Delta Y = S \cdot \sin \alpha$$

$$\cos \alpha = \frac{\Delta X}{S} \rightarrow \Delta X = S \cdot \cos \alpha$$



$$Y_B = Y_A + \Delta Y = Y_A + S \cdot \sin \alpha$$

$$X_B = X_A + \Delta X = X_A + S \cdot \cos \alpha$$

# Fundamental Computation - 1

## EXAMPLE - 1

Known:

- ▶ A ( $Y_A = 9417.41 \text{ m}$  ;  $X_A = 8418.62 \text{ m}$ )
- ▶  $S_{AB} = 94.17 \text{ m}$  ,  $t_{AB} = \alpha = 347^g .3540$

Unknown:

$$B (Y_B ; X_B ) = ???$$

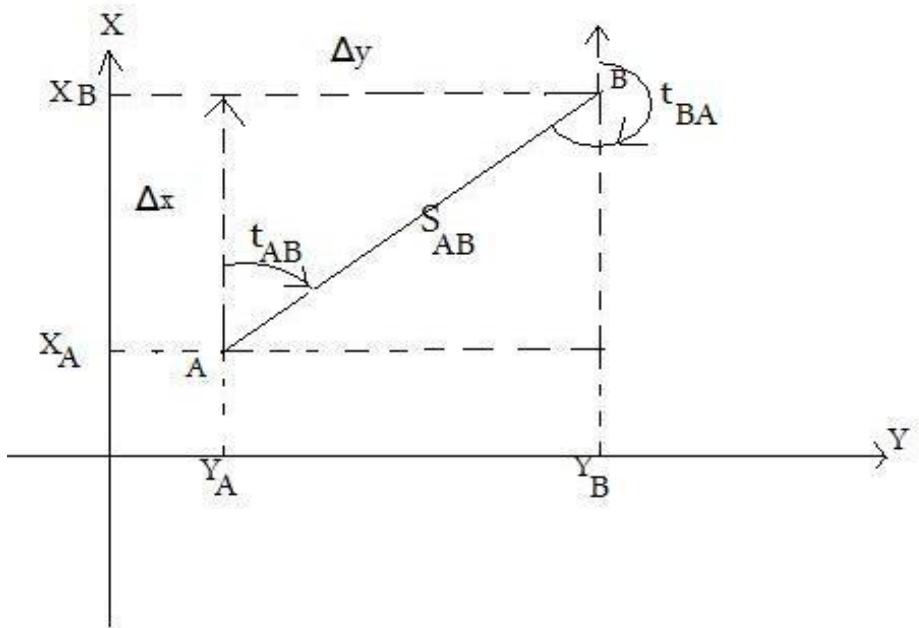
- ▶  $Y_B = 9417.41 + (94.17 * \sin(347.3540)) = 9417.41 + 69.30 = 9348.11 \text{ m}$
- ▶  $X_B = 8418.62 + (94.17 * \cos(347.3540)) = 8418.62 + 63.76 = 8482.38 \text{ m}$

# Fundamental Computation - 2

Known: A ( $X_A, Y_A$ )  
B ( $X_B, Y_B$ )

Unknown:  $S_{AB}$ ,  $t_{AB}$ ,  $t_{BA}$

$$\begin{aligned}\Delta Y &= Y_B - Y_A \\ \Delta X &= X_B - X_A\end{aligned}$$



$$\tan(AB) = \frac{Y_B - Y_A}{X_B - X_A} \rightarrow (AB) = \arctan \frac{Y_B - Y_A}{X_B - X_A} = \arctan \frac{\Delta Y}{\Delta X} = \text{atn} \frac{\Delta Y}{\Delta X}$$

$$AB = S = \sqrt{\Delta Y^2 + \Delta X^2}$$

# Fundamental Computation - 2

$$\tan t_{AB} = \frac{\Delta Y_{AB}}{\Delta X_{AB}}$$

This equation is used for calculating the azimuth in first quadrant.

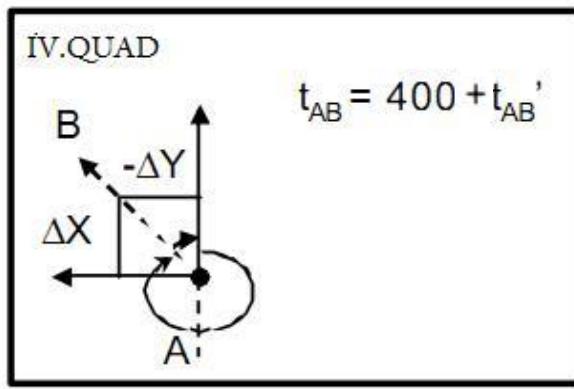
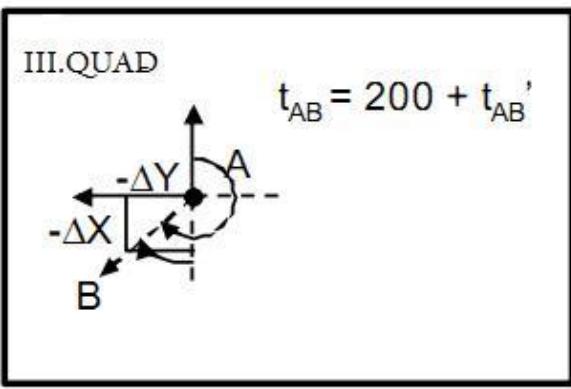
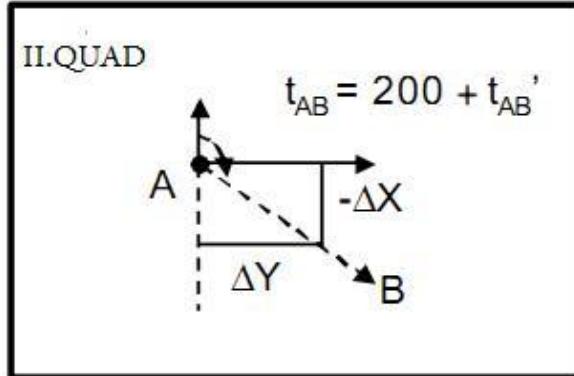
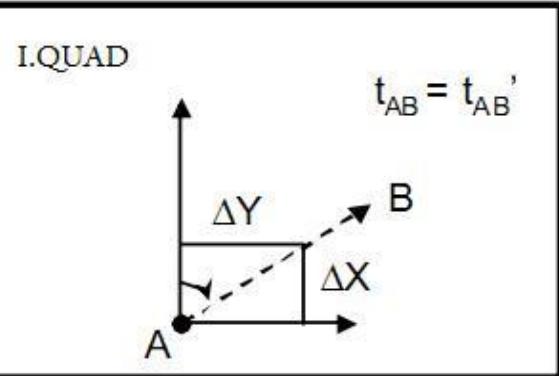
$$t_{AB} = \arctan\left(\frac{\Delta Y_{AB}}{\Delta X_{AB}}\right)$$

---

$$t'_{AB} = \arctan\left(\frac{\Delta Y_{AB}}{\Delta X_{AB}}\right)$$

QUADRANT	$\Delta y / \Delta x$	Azimuth
FIRST QUADRANT	+ / +	$t = t'$
SECOND QUADRANT	+ / -	$t = 200^g + t'$
THIRD QUADRANT	- / -	$t = 200^g + t'$
FOURTH QUADRANT	- / +	$t = 400^g + t'$

# Fundamental Computation - 2



# Fundamental Computation - 2

## EXAMPLE - 2

$$Y_A = 500 \text{ m}, \quad Y_B = 675 \text{ m}$$

$$X_A = 500 \text{ m}, \quad X_B = 620 \text{ m}$$

$$(AB) = ?$$

$$AB = S = ?$$

$$(AB) = \operatorname{atn} \frac{Y_B - Y_A}{X_B - X_A} = \operatorname{atn} \frac{675 - 500}{620 - 500} = \operatorname{atn} = \frac{175}{120} \rightarrow \alpha = 61^g.7345$$

$$(AB) = \alpha = 61^g.7345$$

$$AB = \sqrt{\Delta Y^2 + \Delta X^2} = \sqrt{175^2 + 120^2} = 212.19 \text{ m}$$

# Fundamental Computation - 2

## EXAMPLE - 3

$$Y_A = 500 \text{ m}, \quad Y_B = 650 \text{ m}$$

$$X_A = 500 \text{ m}, \quad X_B = 425 \text{ m}$$

$$(AB) = ?$$

$$AB = S = ?$$

$$(AB) = \operatorname{atn} \frac{Y_B - Y_A}{X_B - X_A} = \operatorname{atn} \frac{650 - 500}{425 - 500} = \operatorname{atn} = \frac{150}{-75} \rightarrow \alpha = -70^g.4833$$

$$(AB) = \alpha + 200 = -70^g.4833 + 200 = 129^g.5167$$

$$AB = \sqrt{\Delta Y^2 + \Delta X^2} = \sqrt{150^2 + (-75)^2} = 167.71 \text{ m}$$

# Fundamental Computation - 2

## EXAMPLE - 4

$$Y_A = 500 \text{ m}, \quad Y_B = 330 \text{ m}$$

$$X_A = 500 \text{ m}, \quad X_B = 425 \text{ m}$$

$$(AB) = ?$$

$$AB = S = ?$$

$$(AB) = \operatorname{atn} \frac{Y_B - Y_A}{X_B - X_A} = \operatorname{atn} \frac{330 - 500}{425 - 500} = \operatorname{atn} = \frac{-170}{-75} \rightarrow \alpha = 73^{\circ}.5490$$

$$(AB) = \alpha + 200 = 73^{\circ}.5490 + 200 = 273^{\circ}.5490$$

$$AB = \sqrt{\Delta Y^2 + \Delta X^2} = \sqrt{(-170)^2 + (-75)^2} = 185.81 \text{ m}$$

# Fundamental Computation - 2

## EXAMPLE - 5

$$Y_A = 500 \text{ m}, \quad Y_B = 330 \text{ m}$$

$$X_A = 500 \text{ m}, \quad X_B = 620 \text{ m}$$

$$(AB) = ?$$

$$AB = S = ?$$

$$(AB) = \operatorname{atn} \frac{Y_B - Y_A}{X_B - X_A} = \operatorname{atn} \frac{330 - 500}{620 - 500} = \operatorname{atn} = \frac{-170}{120} \rightarrow \alpha = -60^{\circ}.8693$$

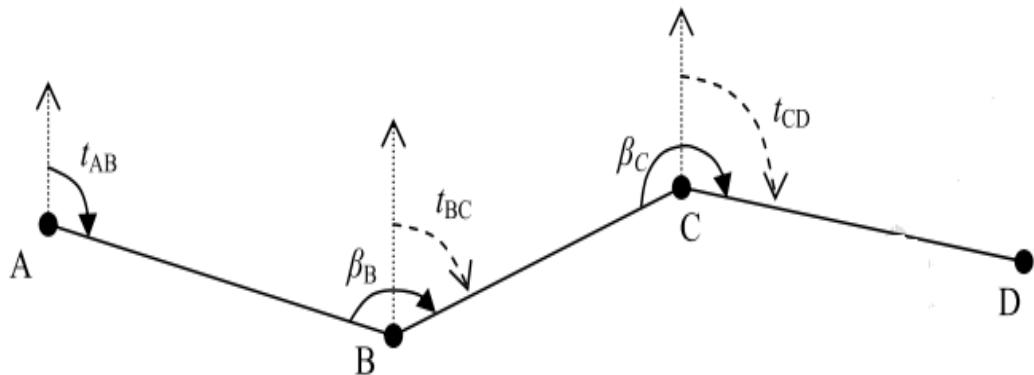
$$(AB) = \alpha + 200 = -60^{\circ}.8693 + 400 = 339^{\circ}.1307$$

$$AB = \sqrt{\Delta Y^2 + \Delta X^2} = \sqrt{(-170)^2 + 120^2} = 208.09 \text{ m}$$

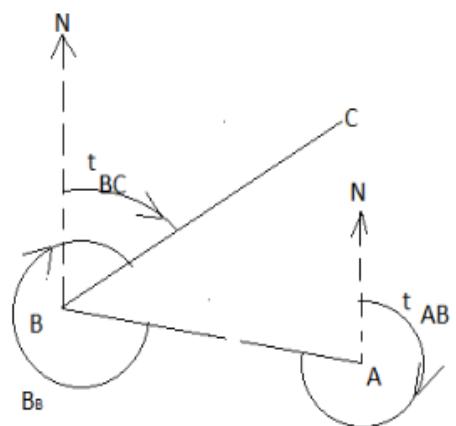
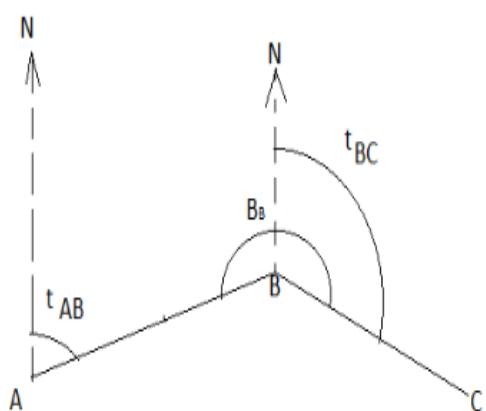
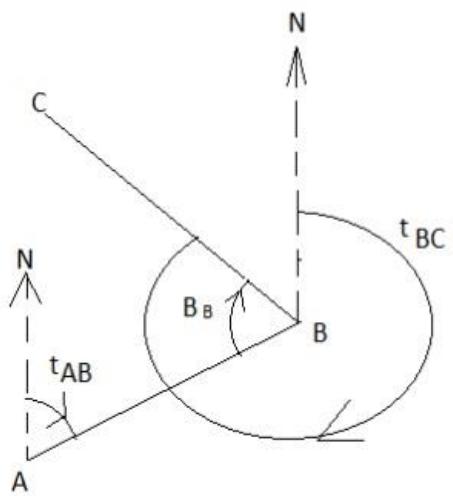
# Fundamental Computation - 3

## Relation Between Azimuth and Traverse Angles

Known:  
 $t_{AB}, \beta_B$   
Unknown:  
 $t_{BC}$



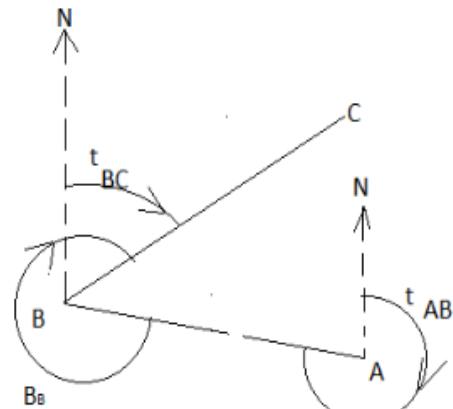
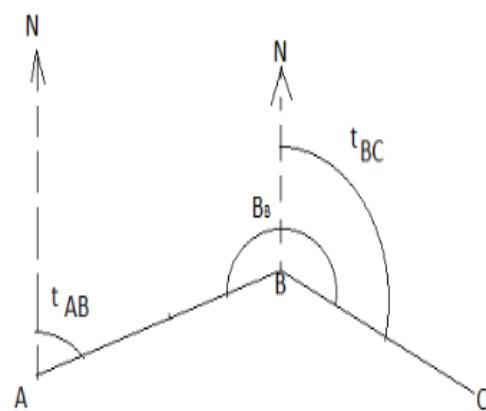
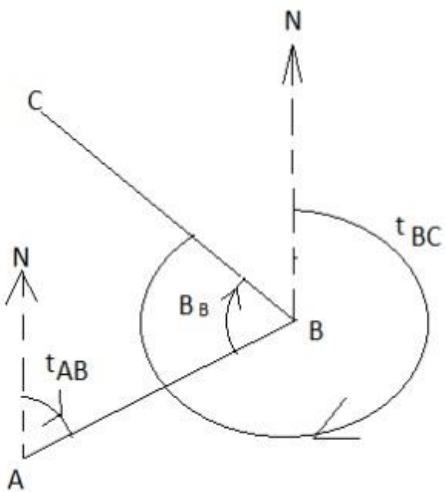
# Fundamental Computation - 3



# Fundamental Computation - 3

$$t_{AB} + \beta_B = K$$

- $K < 200^g$ ;  $K + 200^g$ ;  $t_{BC} = t_{AB} + \beta_B + 200^g$
- $200^g < K < 600^g$ ;  $K - 200^g$ ;  $t_{BC} = t_{AB} + \beta_B - 200^g$
- $K > 600^g$ ;  $K - 600^g$ ;  $t_{BC} = t_{AB} + \beta_B - 600^g$



# Fundamental Computation - 3

## EXAMPLE - 6

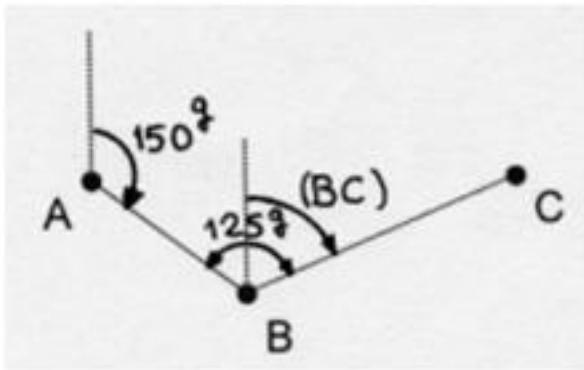
Known

$$(AB) = 150^g$$

$$\beta = 125^g$$

Unknown

$$(BC) = ?$$



$$(BC) = (AB) + \beta \pm 200^g = 150^g + 125^g \pm 200^g = 275^g - 200^g = 75^g$$

# Fundamental Computation - 3

## EXAMPLE - 7

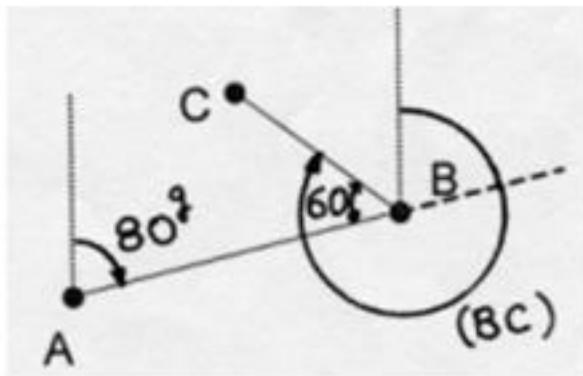
Known

$$(AB) = 80^g$$

$$\beta = 60^g$$

Unknown

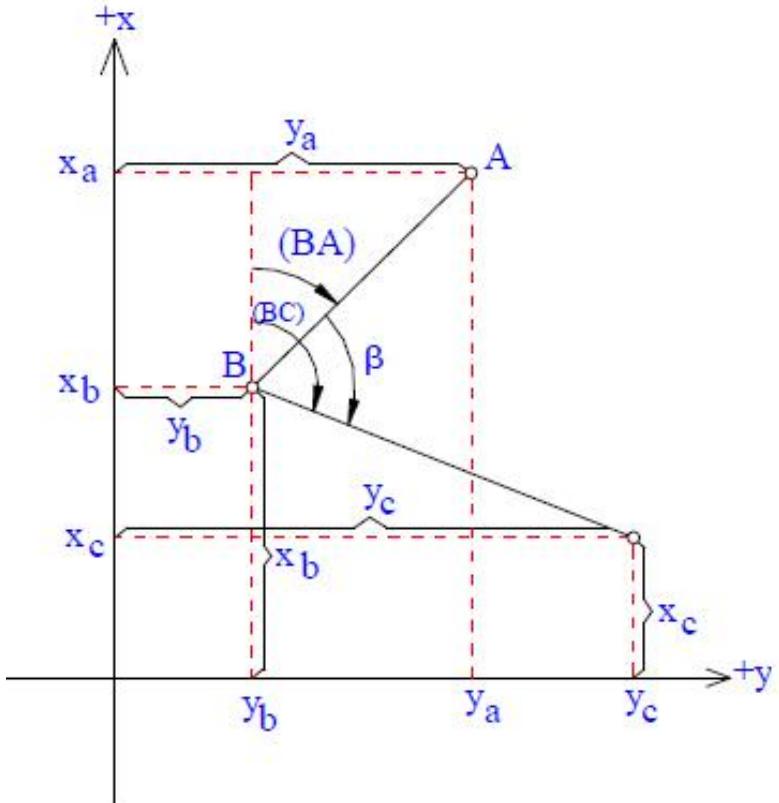
$$(BC) = ?$$



$$(BC) = (AB) + \beta \pm 200^g = 80^g + 60^g \pm 200^g = 140^g + 200^g = 340^g$$

# Fundamental Computation - 4

## Relation Between Azimuth and Traverse Angles



Known

A (Y,X)  
B (Y,X)  
C (Y,X)

Unknown

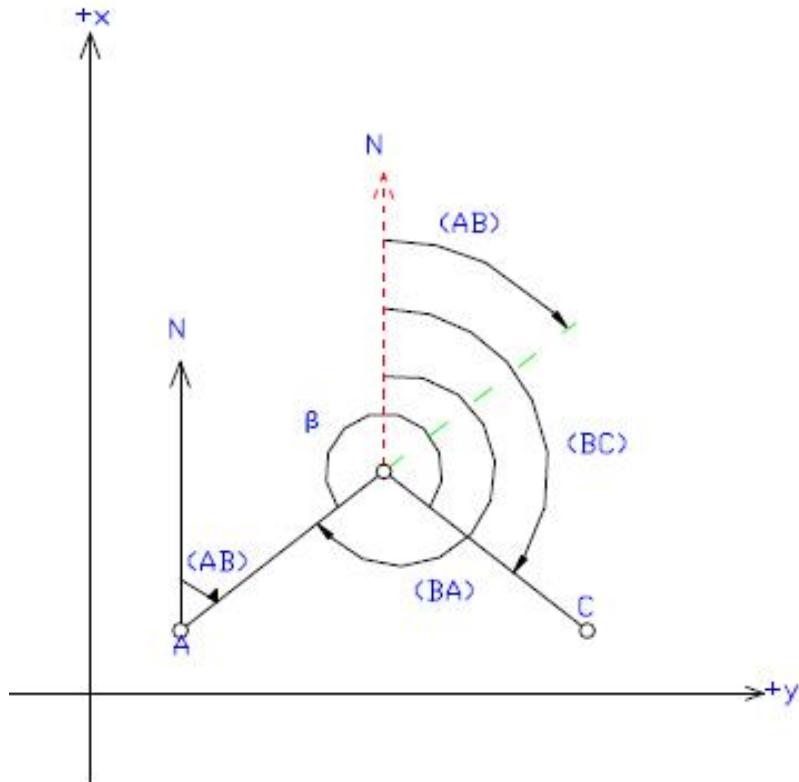
$$\beta = ?$$

$$\beta = (BC) - (BA)$$

$$(BC) = \text{atn} \frac{Y_C - Y_B}{X_C - X_B}$$

$$(BA) = \text{atn} \frac{Y_A - Y_B}{X_A - X_B}$$

# Fundamental Computation - 4



Known

A (Y,X)  
B (Y,X)  
C (Y,X)

Unknown

$\beta = ?$

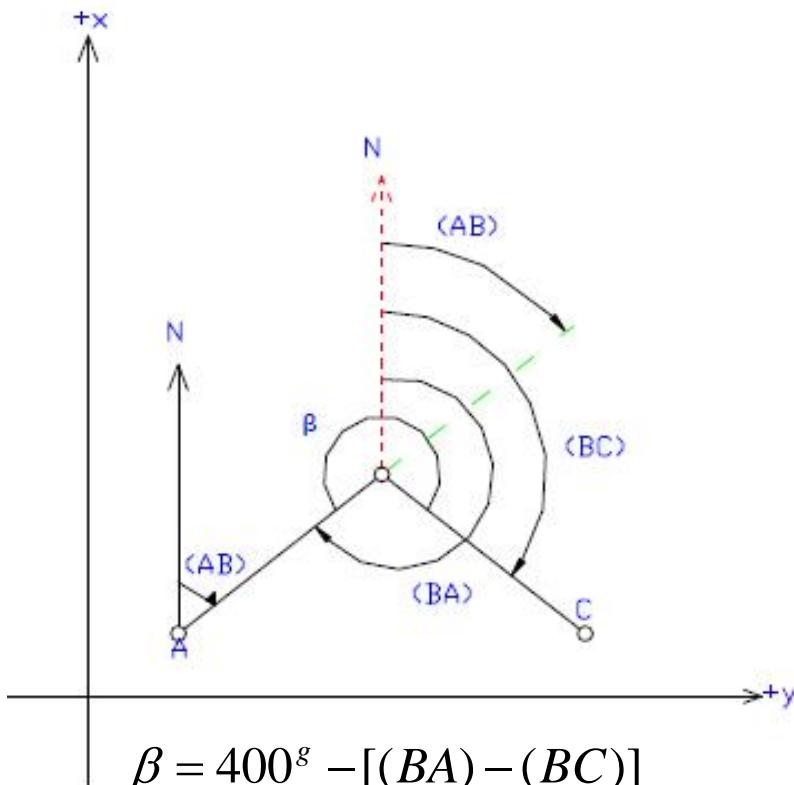
$$\beta = 400^g - [(BA) - (BC)]$$

$$(BC) = \text{atn} \frac{Y_C - Y_B}{X_C - X_B}$$

$$(BA) = \text{atn} \frac{Y_A - Y_B}{X_A - X_B}$$

# Fundamental Computation - 4

## EXAMPLE - 7



$$(BC) = \operatorname{atn} \frac{Y_C - Y_B}{X_C - X_B}$$

$$(BA) = \operatorname{atn} \frac{Y_A - Y_B}{X_A - X_B}$$

Nokta	Y	X
A	585 m	640 m
B	650 m	530 m
C	755 m	465 m

$$\beta = ?$$

$$(BC) = \operatorname{atn} \frac{Y_C - Y_B}{X_C - X_B} = \operatorname{atn} \frac{755 - 650}{465 - 530} = \operatorname{atn} \frac{105}{-65} = -64^g.7117$$

$$(BC) = -64^g.7117 + 200^g = 135^g.2883$$

$$(BA) = \operatorname{atn} \frac{Y_A - Y_B}{X_A - X_B} = \operatorname{atn} \frac{585 - 650}{640 - 530} = \operatorname{atn} \frac{-65}{110} = -33^g.9769$$

$$(BA) = -33^g.9769 + 400^g = 366^g.0231$$

$$\beta = 400^g - [366.0231 - 135.2883]$$

$$\beta = 169^g.2652$$

# Week-7

## Traverse Computations