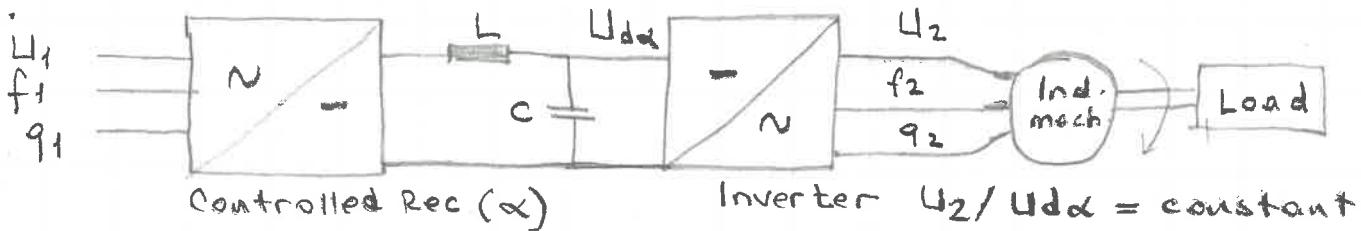


Switch mode dc to ac inverters are used in ac motor drives and uninterruptible ac power supplies where the objective is to produce a sinusoidal ac output whose magnitude and frequency can both be controlled.

This is important for adjustable speed control of ac drives. In order not to decrease torque capability of ac drives, we must keep $\frac{V}{f}$ rate constant. For this reason we must have the ability to change both voltage and frequency simultaneously.

Let me look over different structures for adjustable dc drives with chronological approach

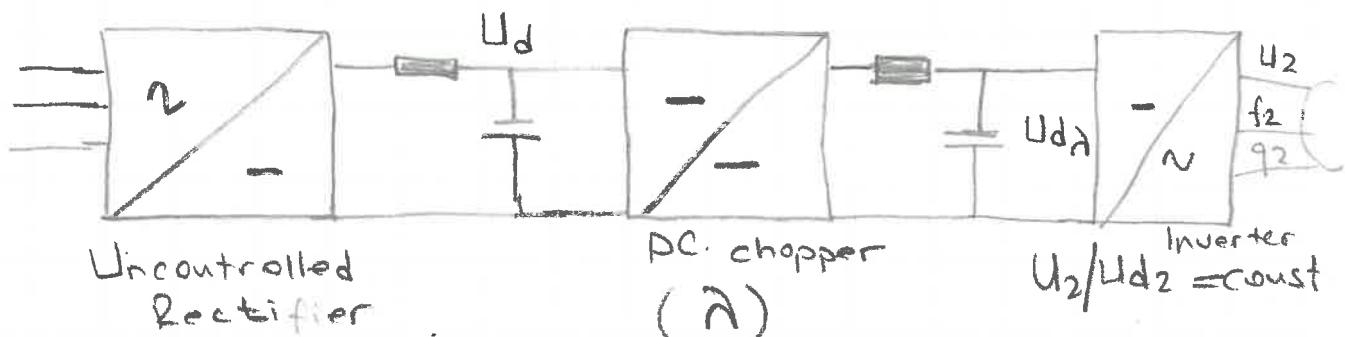
1.



- Higher harmonic distortion
- Higher reactive power consumption
- Voltage is controlled via controlled rectifier

Frequency is " via inverter

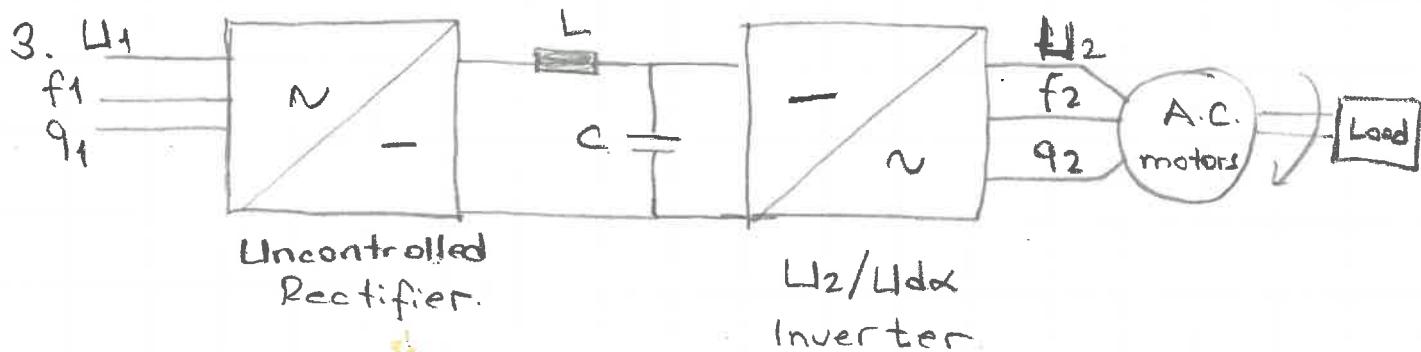
2.



$$\alpha = 0$$

- Lower harmonic distortion
- Lower reactive power consumption
- Higher cost

- Voltage is adjusted via dc chopper
- Frequency is adjusted via inverter.



- * Lower cost
- * Lower harmonic distortion
- * // reactive power consumption
- * Both voltage and frequency are adjusted via inverter
- * thanks to PWM control method, output voltage wave is close to sinusoidal wave.

There are different ^{types} _{dc-ac} converters based on some parameters.

1. For supply source

- Voltage source inverters
- Current " "

2. According to the number of phases

- Single phase
- Three phase

3 According to control method

- Rectangular wave inverter
- Partial rectangular wave inverter
- PWM inverter

- d) According to circuit structure of single phase inverter
- Half bridge inverter
 - Full bridge inverter
 - push-pull inverter

SINOSOIDAL PWM

In inverter circuits, the PWM is a bit more complex. why? We would like to the inverter output to be sinusoidal with magnitude and frequency controllable.

In order to produce a sinusoidal output voltage waveform at the desired frequency; a sinusoidal control signal at desired frequency is compared with a triangular waveform.

The frequency of the triangular waveform establishes the inverter switching frequency f_s and is kept constant along with its amplitude V_{tri} .

f_s is also called the carrier frequency.

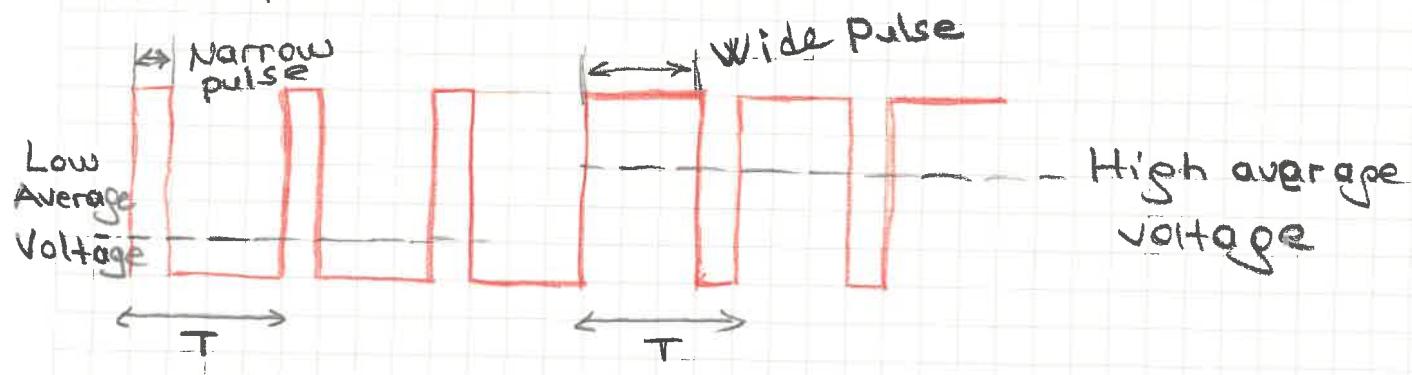
The control signal $V_{control}$ is used to modulate the switch duty ratio. It has f_1 frequency which is the desired fundamental frequency of the inverter voltage output.

It is recognized that the inverter output voltage will not be perfect sinusoidal wave and will contain voltage components at harmonic frequencies of f_1 .

PULSE - WIDTH MODULATION

Pulse-width modulation is a powerful technique for controlling analog circuits with a controller's digital outputs. In many applications such as from communication to power control PWM is used widely. It is a modulation process with a series of on and off pulses and varying duty cycle.

From the point of motor control, the power to be applied to the motor can be controlled by varying voltage at motor terminals. The voltage is controlled by changing the timing of these pulses.



The longer the pulse is on, the faster the motor will rotate. The shorter the pulse is on, the slower the motor will rotate.

In other approach, the wider pulse width, the more average voltage is applied to motor terminals in order to increase magnetic flux level.

Frequency Modulation Ratio (M_f)

$$M_f = \frac{f_s}{f_1}$$

f_s = frequency of carrier signal

f_1 = frequency of control signal

Important Issues for M_f

- * M_f must be integer (otherwise harmonic content will be higher).
- * If M_f is equal to three and its triples like 6, 9, ... 3rd harmonic will be eliminated in line values (not phase voltage)
- * M_f value is increased, harmonic reduces to lower values. But in this case, since switching frequency increases, the switching power losses will be higher. For this reason, an optimisation process is needed seriously.

Amplitude Modulation Ratio (M_a)

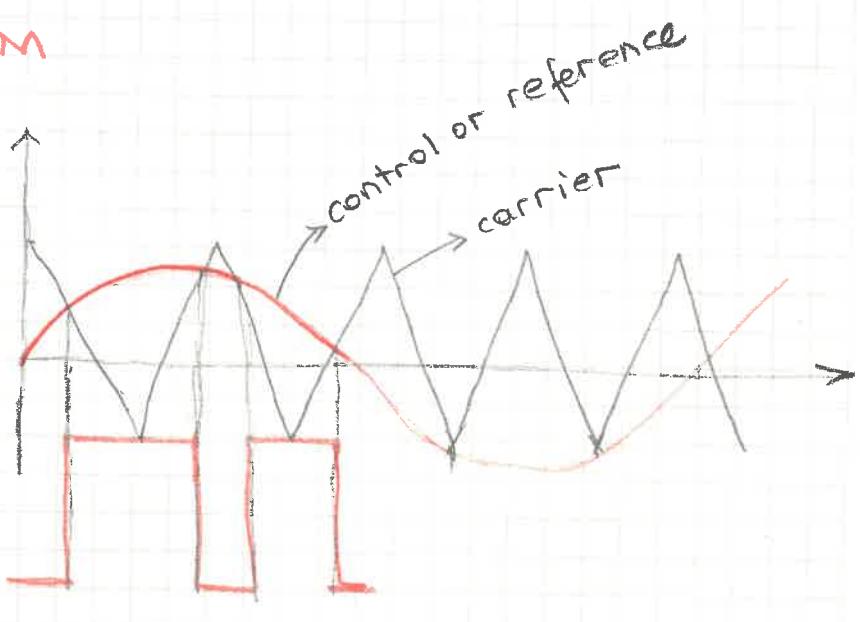
$$M_a = \frac{\text{Peak value of control signal}}{\text{Peak value of carrier signal.}}$$



SINUSOIDAL PWM

In order to control the output voltage and frequency of inverter,

Modulation magnitude and frequency are changed.



- * The carrier frequency determines the switching frequency of inverter.

- * The control frequency determines the frequency of output signal.

In inverter logic, the switches of A phase, S_{A+} and S_{A-} are controlled based on the comparison of $V_{control}$ and $V_{carrier}$ as independent of the direction of current:

- * If $V_{control} > V_{carrier}$ S_{A+} is ON → means $V_{output} = \frac{1}{2}V_{dc}$ or $V_{output} = V_{dc}$ dependent on half-bridge or full-bridge.

- * If $V_{control} < V_{carrier}$ S_{A-} is ON → means

$V_{output} = -\frac{1}{2}V_{dc}$ or $-V_{dc}$ dependent on half-bridge or full-bridge connection.

- * if $0 \leq Ma \leq 1$, fundamental component peak value $VA_1 = Ma \cdot \frac{V_{dc}}{2}$
- * if $Ma = 1$, $VA_1 = \frac{V_{dc}}{2}$ as a max value. It means that max. output voltage value of inverter is obtained.
- * if $Ma > 1$, this region is called as over-modulation region

The operation in the over-modulation region contains more harmonics as compared to linear region

Major drawback of sinusoidal PWM is that max Ma value is 0.785. It means 78.5% of inverter capacity can be used only. In order to increase this value different PWM methods had been developed like the third harmonic injection PWM or space vector PWM(SV-PWM).

Third harmonic injection method increases this value to 90.7%. But it requires much more calculation in the memory of microcontroller.

Space Vector PWM obtains the same score with 90.7%. In addition, since only one power switch is switched in any time, the switching losses are diminished by making inverter more efficient.

FOR HALF BRIDGE INVERTER

The analysis of the DC-AC inverters is done taking into accounts the following assumptions

- 1- The current entering terminal voltage is considered positive
- 2- The switches are unidirectional
- 3- The current i_a is the same for the power switches.

$$S_1 \text{ is on} \quad 0 < t \leq T_1 \quad V_o = \frac{V_{in}}{2} = \frac{V_{dc}}{2}$$

$$S_4 \text{ is on} \quad T_1 \leq t < T_2 \quad V_o = -\frac{V_{in}}{2} = -\frac{V_{dc}}{2}$$

$$V_a = \sqrt{\frac{1}{\pi} \int_0^{\pi} \left(\frac{V_{dc}}{2}\right)^2 \cdot d(\omega t)}$$

$$V_a = \frac{V_{dc}}{2} \text{ rms voltage value}$$

$$V_{a1} = 2 \cdot \frac{1}{\pi} \int_0^{\pi} \frac{V_{dc}}{2} \cdot \sin(\omega t) \cdot d(\omega t)$$

$$V_{a1} = \frac{2\sqrt{2}}{\pi} \cdot \frac{V_{dc}}{2} \quad \text{Fundamental component voltage value}$$

FOR FULL BRIDGE INVERTER

When the switches S_1 and S_2 are turned on simultaneously for a duration $0 < t \leq T_1$ (S_4 and S_3 are off) $V_{ab} = V_{dc}$.

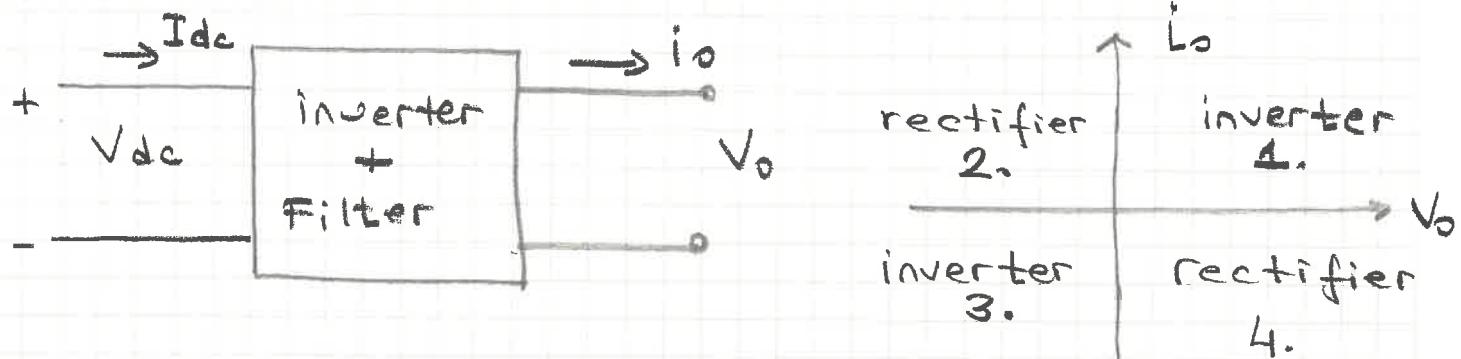
When the switches S_3 and S_4 are turned on simultaneously for a duration $T_1 \leq t \leq T_2$

$$V_{ab} = -V_{dc}$$

$V_{ab} = V_{dc}$, rms voltage value.

$$V_{ab1} = \frac{2\sqrt{2}}{\pi} \cdot U_d \quad \text{Fundamental component voltage value}$$

Power Flow for inverters



Any inverter operates as rectifier when the power flow is from the load to the electricity network.

Example

A half bridge inverter with 300V and 50Hz supplies to a 15Ω resistor. By omitting the circuit losses:

- Find out V_{rms} , I_{rms} and power of the load
- Find out input current and rms and average current value passing from each transistor.

$$V_a = \frac{V_{dc}}{2} \text{ for half bridge} \quad I_a = \frac{V_a}{R} = \frac{150}{15} = 10 \text{ A.}$$

$$= \frac{300}{2} = 150 \text{ V.}$$

$$P = \frac{V_a^2}{R} = 1500 \text{ W.}$$

$$b) \quad I_i = \frac{V_{dc}/2}{R} = 10 \text{ A} \quad I_{TAV} = \frac{I_i}{2} = 5 \text{ A}$$

$$I_{Trms} = \frac{I_i}{\sqrt{2}} = 7.07 \text{ A.}$$

Example

An induction motor is controlled via SPWM inverter. The parameters of motor are given as following:

$$P = 2.2 \text{ kW} \quad n = 1400 \text{ rpm} \quad U = 380 \text{ V} \quad I = 5 \text{ A} \quad f = 50 \text{ Hz}$$

$$\cos \phi = 0.78 \quad p = 2 \quad R_1 = 2.39 \Omega, \quad R_2' = 2.13 \Omega$$

$$X_1 = 15.4 \Omega \quad X_2' = 12.13 \Omega \quad \text{Y connected. } 3\text{~N}$$

a) For nominal operation Find out synchronous speed, slip, torque and efficiency.

b) For nominal current Loading, When the output of inverter is 190V, 25 Hz, find out slip and speed of motor.

$$a) \quad n_s = \frac{60 \cdot f_1}{P} = \frac{60 \cdot 50}{2} = 1500 \text{ rpm} \quad s = \frac{n_s - n}{n_s}$$

$$s = \frac{1500 - 1400}{1500} = 0.066 \quad P_i = P_{elec} = \sqrt{3} \cdot U \cdot I \cdot \cos \phi \\ P_i = \sqrt{3} \cdot 380 \cdot 5 \cdot 0.78 = 2566 \text{ W.}$$

$$T = \frac{P_{mech}}{\omega} = \frac{P_{mech}}{\frac{2\pi \cdot n}{60}} = \frac{2200}{2\pi \cdot \frac{1400}{60}} = 15 \text{ Nm.}$$

$$\eta = \frac{P_o}{P_{in}} = \frac{P_{mech}}{P_{elec}} = \frac{2200}{2566} = 85 \%$$

$$b) \quad I = \frac{U/\sqrt{3}}{Z} = \frac{190/\sqrt{3}}{\sqrt{(2.39 + \frac{2.13}{s})^2 + [(15.4) + 12.3] \cdot \frac{25}{50}}} \quad$$

$$Z = \frac{190/\sqrt{3}}{5A} = 21.99 \Omega \Rightarrow s = 0.144$$

$$n_s = \frac{60 \cdot f_1}{P} = \frac{60 \cdot 25}{2} = 750 \text{ rpm.}$$

$$n = (1-s) \cdot n_s \Rightarrow n = 642 \text{ rpm.}$$

RL yüklü üç fazlı tam köprü bağıltılı eviricide.

$R = 10\Omega$ $L = 20 \text{ mH}$ $m_a = 0.8$, $f_{\text{sin}} = 60 \text{ Hz}$,

$f_{\text{tri}} = 1260 \text{ Hz}$ ve $V_{\text{dc}} = 100 \text{ V}$ 'tur.

- a) Çıkış geriliğinin ve akımının temel bileşenini bulunuz
- b) En tehlikeli 3 harmonik için THD değerini akım için bulunuz. ($I_{5,\text{rms}} = 0.36$, $I_{7,\text{rms}} = 0.11$, $I_{11,\text{rms}} = 0.09 \text{ A}$)

$$m_a = \frac{V_1}{V_{\text{dc}}} \Rightarrow V_1 = 0.8 \cdot 100 = 80 \text{ V.}$$

$$I_n = \frac{V_n}{Z_n} = \frac{V_n}{\sqrt{R^2 + (n2\pi f \cdot L)^2}} = \frac{80}{\sqrt{10^2 + (1 \cdot 2\pi 60 \cdot 0.02)^2}}$$

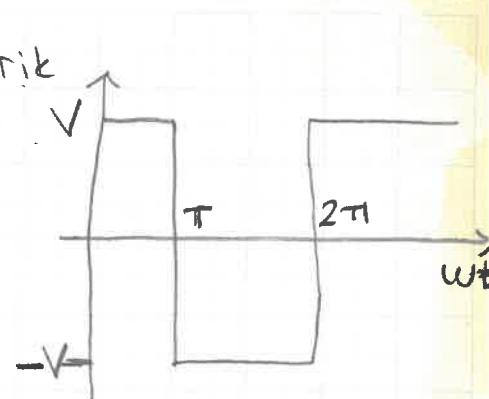
$$I_n = 6.39 \text{ A} = I_1$$

$$I_{1,\text{rms}} = 6.39 / \sqrt{2} = 4.52 \text{ A.}$$

$$\text{b) THD.} = \sqrt{\sum_{n=2}^{\infty} I_{n,\text{rms}}^2} = \sqrt{\frac{0.11^2 + 0.36^2 + 0.09^2}{4.52}}$$

$$\text{THD} = \% 8.7$$

Şekildeki kare dalganın trigonometrik Fourier serisini bularak çizgisel spektrumunu çiziniz?



Bu fonksiyon simetrikdir.

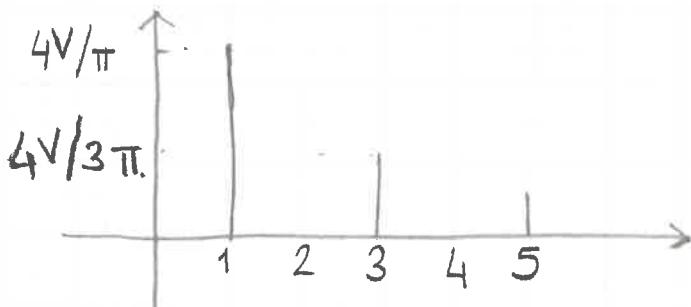
Bu nedenle $a_0 = 0$ dir
single function and an

$f(t) = -f(-t)$ cos terimler seride bulunmaz. Fonksiyon tek fonksiyondur. Dolayısıyla sadece b_n katsayıları bulunur.

$$b_n = \frac{1}{\pi} \left[\int_0^{\pi} V \cdot \sin nwt \cdot d(wt) + \int_{\pi}^{2\pi} (-V) \cdot \sin nwt \cdot d(wt) \right]$$

$$= \frac{V}{\pi} \left\{ \left[-\frac{1}{n} \cdot \cos nwt \right]_0^{\pi} + \left[\frac{1}{n} \cos nwt \right]_{\pi}^{2\pi} \right\}$$

$$b_n = \frac{V}{n \cdot \pi} (-\cos n\pi + \cos 0 + \cos n2\pi - \cos n\pi) = \frac{2V}{\pi n} (1 - \cos n\pi)$$



$$f(t) = \frac{4V}{\pi} \cdot \sin \omega t + \frac{4V}{3\pi} \cdot \sin 3\omega t + \frac{4V}{5\pi} \cdot \sin 5\omega t$$