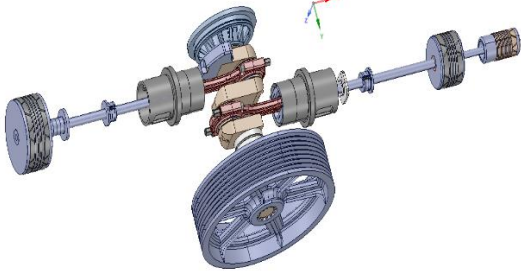
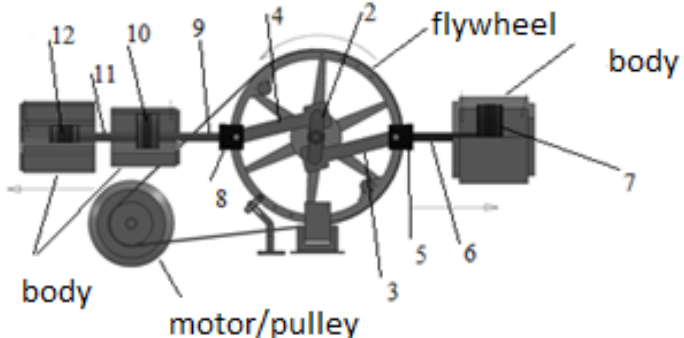
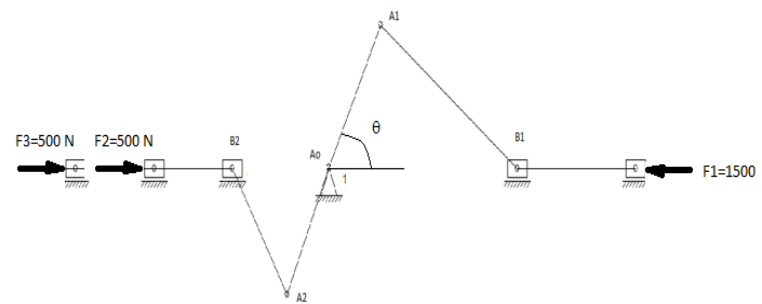


MACHINE DYNAMICS

Homework, May 8, 2019

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| Name Surname | | Signature | |
| Student Number | | Group Number | |

QUESTION 1

| | | | | | | | | | | | | | | | | | | | | | | | | |
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| | | | | | | | | | | | | | | | | | | | | | | | | |
| <table><tr><td>2</td><td>crank</td></tr><tr><td>3</td><td>connecting rod for 1st stage</td></tr><tr><td>4</td><td>connecting rod for 2nd stage</td></tr><tr><td>5</td><td>cross head for 1st stage</td></tr><tr><td>6</td><td>piston rod for 1st stage</td></tr><tr><td>7</td><td>piston for 1st stage</td></tr><tr><td>8</td><td>cross head for 2nd and 3rd stages</td></tr><tr><td>9</td><td>piston rod for 2nd stage</td></tr><tr><td>10</td><td>piston for 2nd stage</td></tr><tr><td>11</td><td>piston rod for 3rd stage</td></tr><tr><td>12</td><td>piston for 3rd stage</td></tr></table> | 2 | crank | 3 | connecting rod for 1 st stage | 4 | connecting rod for 2 nd stage | 5 | cross head for 1 st stage | 6 | piston rod for 1 st stage | 7 | piston for 1 st stage | 8 | cross head for 2 nd and 3 rd stages | 9 | piston rod for 2 nd stage | 10 | piston for 2 nd stage | 11 | piston rod for 3 rd stage | 12 | piston for 3 rd stage | |  |
| 2 | crank | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | connecting rod for 1 st stage | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | connecting rod for 2 nd stage | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | cross head for 1 st stage | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | piston rod for 1 st stage | | | | | | | | | | | | | | | | | | | | | | | |
| 7 | piston for 1 st stage | | | | | | | | | | | | | | | | | | | | | | | |
| 8 | cross head for 2 nd and 3 rd stages | | | | | | | | | | | | | | | | | | | | | | | |
| 9 | piston rod for 2 nd stage | | | | | | | | | | | | | | | | | | | | | | | |
| 10 | piston for 2 nd stage | | | | | | | | | | | | | | | | | | | | | | | |
| 11 | piston rod for 3 rd stage | | | | | | | | | | | | | | | | | | | | | | | |
| 12 | piston for 3 rd stage | | | | | | | | | | | | | | | | | | | | | | | |
| <table><tr><td>For each connecting rod: $M_{\text{connecting rod}}=36 \text{ kg}$</td><td>$M_{\text{crank}}=250 \text{ kg}$</td></tr><tr><td>For each cross head: $M_{\text{cross head}}=17 \text{ kg}$</td><td>$M_{\text{piston (1st stage)}}=40 \text{ kg}$</td></tr><tr><td>For each piston rod: $M_{\text{piston rod}}=22 \text{ kg}$</td><td>$M_{\text{piston (2nd stage)}}=20 \text{ kg}$</td></tr><tr><td></td><td>$M_{\text{piston (3rd stage)}}=10 \text{ kg}$</td></tr></table> | | For each connecting rod: $M_{\text{connecting rod}}=36 \text{ kg}$ | $M_{\text{crank}}=250 \text{ kg}$ | For each cross head: $M_{\text{cross head}}=17 \text{ kg}$ | $M_{\text{piston (1st stage)}}=40 \text{ kg}$ | For each piston rod: $M_{\text{piston rod}}=22 \text{ kg}$ | $M_{\text{piston (2nd stage)}}=20 \text{ kg}$ | | $M_{\text{piston (3rd stage)}}=10 \text{ kg}$ | <p>For the given multistage compressor,</p> <ol style="list-style-type: none">Obtain the dynamic equivalent model of the system by performing mass reduction by considering 2 or 3 substantial points for each link.Find the reduced mass moment of inertia to motor shaft?Obtain the equation of motion of the system. <p>Note: The bars are homogenous and center of mass of each link is the midpoint.</p> <p>Roadmap: 1. Reduce the each stage to crankpin (The reduced mass to point A) 2. Write the reduced mass moment of inertia to flywheel shaft and motor shaft, respectively.</p> | | | | | | | | | | | | | | |
| For each connecting rod: $M_{\text{connecting rod}}=36 \text{ kg}$ | $M_{\text{crank}}=250 \text{ kg}$ | | | | | | | | | | | | | | | | | | | | | | | |
| For each cross head: $M_{\text{cross head}}=17 \text{ kg}$ | $M_{\text{piston (1st stage)}}=40 \text{ kg}$ | | | | | | | | | | | | | | | | | | | | | | | |
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| | $M_{\text{piston (3rd stage)}}=10 \text{ kg}$ | | | | | | | | | | | | | | | | | | | | | | | |
| <p>For velocity of the piston:</p> $x = r \cos \theta + \left(L \left(1 - \frac{r^2}{2L^2} \sin^2 \theta \right) \right)$ <p>where r is crank rod and L is the connecting rod.</p> | | | | | | | | | | | | | | | | | | | | | | | | |

QUESTION 2)

For the given position of the mechanism; determine the required **tork** for **static equilibrium** of the system by considering the acting static forces **F₁**, **F₂** and **F₃** by ignoring the inertia forces. Use the kinematic figure by scaling.