

CHAPTER 2

ATMOSPHERIC CONCENTRATION UNITS

MASS

- ✖ Quantity of matter in an object.
- ✖ Default SI unit is kilograms (kg)
- ✖ Other units
 - + Milligrams, micrograms, nanograms (atmospheric concentrations)
 - + Pound-mass ($1 \text{ lb}_m = 0.454 \text{ kg}$)

FORCE

- ✖ Any influence that causes an object to undergo a certain change in its state (movement, direction, shape, etc.)
- ✖ In motion equations
 - + Force is the product of mass of the object and its acceleration (Newton's second law)
- ✖ Units
 - + Newton (kilogram.meters per second square)
 - + Dyn ($1 \text{ N} = 10^5 \text{ dyn}$)
 - + Kilogram-force ($1 \text{ N} = 0.10197 \text{ kp}$)
 - + Pound-force ($1 \text{ N} = 0.22481 \text{ lb}_f$)

PRESSURE

- ✖ The force exerted per unit area in a direction perpendicular to the surface.
- ✖ Two reference systems
 - + Absolute pressure
 - ✖ Total pressure applied to a surface
 - ✖ Total atmospheric pressure at sea level is 1 atm
 - + Gauge pressure
 - ✖ Pressure relative to the local atmospheric pressure
 - ✖ Total pressure minus local atmospheric pressure

PRESSURE

✖ Units

- + Default SI unit is Pa
 - ✖ Newtons per square meter (N/m²)
 - ✖ Atmospheric pressure at sea level is 101325 Pa
- + Other units
 - ✖ Atmospheric pressure unit (atu, atm)
 - ✖ bars (mb)
 - ✖ psi
 - ✖ 1 atm = 1013.25 mb = 101325 Pa
 - ✖ 100 Pa = 1 mb
 - ✖ 1 atm = 14.7 psi

PRESSURE

- ✖ Toricelli experiment
- ✖ Mercury
 - + 1 atm at sea level = 76 cm Hg = 760 mm Hg
- ✖ Water
 - ✖ 1 atm at sea level = 10.33 m H₂O = 1033 cm H₂O
- ✖ Other
 - + Density of ethanol at 20 C = 789 kg/m³
 - + Density of water at 20 C = 998.2 kg/m³
 - + Atmospheric pressure in terms of ethanol column?

TEMPERATURE & HEAT

- ✖ Heat: Total kinetic energy of all atoms and molecules in a matter
- ✖ Temperature: Average kinetic energy of all atoms and molecules in a matter
- ✖ Units:
 - + Degrees Celcius
 - ✖ Water freezes at 0 C, and boils at 100 C
 - + Fahrenheit
 - ✖ Water freezes at 32 F, and boils at 212 F → slope = 1.8:1.0
 - + Kelvin
 - ✖ Water freezes at 273 K, and boils at 373 K → slope = 1.0:1.0

VOLUME

- ✖ The amount of space occupied by an object
- ✖ At any given time space is three-dimensional
 - + Each dimension is measured by a length unit.
 - + Thus, the default unit is cubic length
- ✖ Units
 - + Cubic meters, cubic centimeters, liters, mililiters, etc.
 - + Cubic foot, cubic inch, gallons, barrel, etc.
 - + $1 \text{ m}^3 = 35.315 \text{ ft}^3$
- ✖ Volume changes by changing temperature and pressure

CONCENTRATION UNITS

- ✖ Concentration is the amount of matter (usually pollutant) in unit amount of mixture
- ✖ **Volumetric concentrations**
 - + Usually for gaseous components in a mixture
 - + Parts per million by volume (ppm or ppmv): number of molecules of a pollutant in a million number of molecules of gaseous mixtures
 - + Parts per billion by volume (ppb or ppbv): number of molecules of a pollutant in a billion number of molecules of gaseous mixtures
 - + Parts per trillion by volume (ppt or pptv): number of molecules of a pollutant in a trillion number of molecules of gaseous mixtures

CONCENTRATION UNITS

- ✖ **Volumetric concentrations**
 - + Partial pressure is most commonly used in air pollution field
 - + Partial pressure is a unit of volumetric concentration
 - + **Example:** Partial pressure of benzene in a flue gas is 0.98 mb. What is the ppm concentration? Flue gas pressure is 1013 mb.
 - ✖ $0.98 \text{ mb} / 1013 \text{ mb} * 1000000 = 993 \text{ ppm}$
 - + Comes from ideal gas law.
 - ✖ At constant temperature and pressure, volume of a pollutant is proportional to its number of moles in the mixture
 - + Concentration is the ratio of volume of gaseous pollutant to the total volume of mixture

CONCENTRATION UNITS

× Volumetric concentrations

- + **Example:** What is the partial pressure (in mm Hg) of 1350 ppm of toluene in the flue gas at a pressure of 1 atm.
 - × $1350 / 1000000 * 1 \text{ atm} * (760 \text{ mm Hg} / 1 \text{ atm}) = 1.026 \text{ mm Hg}$
- + Number of moles of a pollutant in unit number of total moles of gaseous mixture is the volumetric concentration of a pollutant.
- + **Example:** A gaseous mixture of 7000 moles contains a mole of m-xylene? What is the concentration of m-xylene in ppm
 - × $1 \text{ mole} / 7000 \text{ moles} * 1000000 = 142.9 \text{ ppm}$
- + The atmosphere is roughly a mixture of oxygen (21% by volume) and nitrogen (79% by volume). The concentration of oxygen is 210000 ppm and of nitrogen is 790000 ppm. Sums up to 1000000 ppm, which is equal to 1.

CONCENTRATION UNITS

× Mass concentrations

- + Mass of a pollutant in unit volume of gaseous mixture
- + Units
 - × Milligrams per cubic meter
 - × Micrograms per cubic meter
 - × Nanograms per cubic meter
 - × Pounds per cubic foot
 - × Pounds per gallon

CONCENTRATION UNITS

✖ Mass concentrations

- + Can be used to express both particulate and gaseous pollutants
- + Mass of a pollutant does not change with temperature
- + Volume of a gaseous mixture changes with both temperature and pressure
- + Thus, mass concentration changes with both temperature and pressure

CONCENTRATION UNITS

✖ Conversion between mass and volumetric concentrations

- + 1 ppm = 1 mg/L?
 - ✖ Only valid for diluted aqueous solutions
 - ✖ Very important
- + In air pollution field, 1 ppm is not equal to 1 mg/L.
- + ppm – mg/m³ conversions are based on ideal gas law
- + **Example:** 100 ppm benzene, 78 g/mole, 25 C, 1 atm, mg/m³?
- + **Example:** 650 ppm toluene, 92 g/mole, 100 C, 1 atm, mg/m³?
- + **Example:** 21% oxygen in atmosphere, 25 C, g/m³?
- + **Example:** 1200 mg/m³ of toluene, 25 C, 92 g/mole, ppm?
- + **Example:** 3300 mg/m³ of SO₂, 150 C, 64 g/mole, ppm?

FLOWRATE

✖ Mass flowrate

- + Mass rate of transfer of a matter through a known cross-section per unit time
- + Units
 - ✖ Milligrams per second
 - ✖ Kilograms per second
 - ✖ Tons per year
 - ✖ Kilograms per hour
 - ✖ Pounds per hour

FLOWRATE

✖ Volumetric flowrate

- + Volume of a gaseous matter transferred through a known cross-section per unit time
- + Units
 - ✖ Cubic meters per second
 - ✖ Liters per second
 - ✖ Cubic meters per hour
 - ✖ Cubic feet per second
 - ✖ Cubic feet per hour

FLOWRATE

✖ Normal and standard conditions

- + Normal conditions: 1 atm, 0 C
- + Standard conditions: 1 atm, 25 C
- + Since volume of a gas changes with temperature and pressure, a standardization is necessary
- + Based on ideal gas law.
- + Units
 - ✖ Nm³/s, Nm³/h
 - ✖ Acfm = actual cubic foot per minute
 - ✖ Scfm = standard cubic foot per minute

FLOWRATE

✖ Normal and standard conditions

- + **Example:** Flue gas of 3500 m³/h at 150 C and 1 atm. What is the flowrate under normal conditions?
 - ✖ $3500 \text{ m}^3/\text{h} \times 273 / 423 = 2259 \text{ Nm}^3/\text{h}$
- + **Example:** Flue gas with a flowrate of 4000 Nm³/h. What is the actual flowrate at 120 C?
 - ✖ $4000 \text{ Nm}^3/\text{h} \times 393 / 273 = 5758 \text{ m}^3/\text{h}$
- + **Example:** Flue gas contains 550 mg/m³ of benzene. What is the concentration under normal conditions if flue gas temperature is 230 C?
 - ✖ $550 \times 303 / 273 = 1013 \text{ mg/Nm}^3$

FLOWRATE

✖ Normal and standard conditions

- + **Example:** Flue gas contains 475 mg/Nm³ of toluene. Flue gas flowrate is 6500 Nm³/h. Temperature is 160 C. Density of flue gas is 0.812 kg/m³. Toluene: 92 g/mole
- + What is the actual concentration?
 - ✖ $475 \text{ mg/Nm}^3 \times 273/433 = 299.5 \text{ mg/m}^3$
- + What is the actual flowrate?
 - ✖ $6500 \times 433/273 = 10309.5 \text{ m}^3/\text{h}$
- + What is the mass flowrate of toluene?
 - ✖ $475 \times 6500 \approx 299.5 \times 10309.5 = 3087500 \text{ mg/h} = 3.088 \text{ kg/h}$
- + What is the mass flowrate of flue gas?
 - ✖ $10309.5 \times 0.812 = 8371.3 \text{ kg/h}$

FLOWRATE

✖ Normal and standard conditions

- + **Example (Cont'd):** Flue gas contains 475 mg/Nm³ of toluene. Flue gas flowrate is 6500 Nm³/h. Temperature is 160 C. Density of flue gas is 0.812 kg/m³. Toluene: 92 g/mole
- + What is the concentration of toluene in ppm?
 - ✖ $0.000475 \times 0.082 \times 273 / 92 = 0.000116 \text{ atm} = 116 \text{ ppm}$

STACK GAS CORRECTIONS

✧ With respect to oxygen concentration

- + To prevent dilution of industrial stack gases with ambient air
- + Legislations set emission standards for 3% oxygen or 6% oxygen

+ Correction:

$$C_c = C_m \frac{21 - R}{21 - M}$$

- + C_c = concentration of pollutant with respect to reference oxygen
- + C_m = concentration of pollutant measured in stack gas
- + R = Percent reference oxygen
- + M = Actual percent oxygen concentration measured in stack gas

STACK GAS CORRECTIONS

✧ With respect to oxygen concentration

- + **Example:** Flue gas contains 450 mg/Nm³ of m-xylene and 6% oxygen. What is the m-xylene concentration wrt 3% oxygen?
 - ✧ $450 * (21 - 3) / (21 - 6) = 540 \text{ mg/Nm}^3$
- + **Example:** Flue gas contains 1200 ppm of benzene and 5.4% of oxygen. What is the benzene concentration wrt 3% oxygen?
 - ✧ $1200 * (21 - 3) / (21 - 5.4) = 1385 \text{ ppm}$

STACK GAS CORRECTIONS

✖ With respect to humidity

- + Legislations usually set emission standards based on dry flue gas

- + Correction:
$$C_c = C_m \frac{100}{100 - H}$$

- + H = Percent humidity measured in stack gas
- + **Example:** Sulfur dioxide concentration in flue gas is 950 mg/Nm³. Humidity is 4.7%. What is the concentration on a dry basis?
- + $950 * 100 / (100 - 4.7) = 997 \text{ mg/Nm}^3$

STACK GAS CORRECTIONS

✖ With respect to temperature

- + Legislations usually set emission standards based on normal conditions, that's 0 C

- + Correction:

$$C_c = C_m \frac{T_m}{T_s}$$

- + T_m = Measured temperature of stack gas in Kelvin
- + T_s = Normal temperature in Kelvin (273 K)
- + **Example:** Sulfur dioxide concentration in flue gas is 840 mg/m³. Temperature is 230 C. What is the normal concentration?
- + $840 * 503 / 273 = 1548 \text{ mg/Nm}^3$

STACK GAS CORRECTIONS

✖ With respect to pressure

- + Legislations usually set emission standards based on normal conditions, that's 1 atm or 1013 mb
- + Correction:

$$C_c = C_m \frac{P_s}{P_m}$$

- + P_m = Measured pressure of stack gas
- + P_s = Normal pressure
- + **Example:** Sulfur dioxide concentration in flue gas is 840 mg/m³. Pressure is 1022 mb. What is the normal concentration?
- + $840 * 1013 / 1022 = 832 \text{ mg/m}^3$

EXAMPLE

- ✖ A flue gas contains 1400 ppm of m-xylene. The flue gas flowrate is 6700 m³/h at 120 C and a pressure of 1023 mb. The oxygen concentration in the flue gas is 5.6% and humidity is 3.8%. The emission standard for m-xylene is 500 mg/Nm³ on a dry basis based on 3% oxygen. M-xylene: 106 g/mole. Density of flue gas under normal conditions is 1.25 kg/m³.
- ✖ What is the flue gas flowrate under normal conditions?
 - + $6700 \text{ m}^3/\text{h} * (273 / 393) * (1023 / 1013) = 4700 \text{ Nm}^3/\text{h}$
- ✖ What is the actual concentration of m-xylene?
 - + $1400/10^6 * 106 / 0.082 / 393 = 0.004605 \text{ g/L} = 4605 \text{ mg/m}^3$

EXAMPLE

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- ✖ What is the concentration under normal conditions?
 - + $4605 \cdot (393 / 273) \cdot (1013 / 1023) = 6564 \text{ mg/Nm}^3$
- ✖ What is the concentration under normal conditions on a dry basis?
 - + $6564 \cdot 100 / (100 - 3.8) = 6823 \text{ mg/Nm}^3$

EXAMPLE

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- ✖ What is the concentration under normal conditions on a dry basis, corrected with respect to 3% reference oxygen?
 - + $6564 \text{ mg/Nm}^3 \cdot (21-3) / (21-5.6) = 7975 \text{ mg/Nm}^3$
- ✖ What is the mass flowrate of m-xylene?
 - + $6564 \text{ mg/Nm}^3 \cdot 4700 \text{ Nm}^3/\text{h} = 3.085 \cdot 10^7 \text{ mg/h} = 30.85 \text{ kg/h}$

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- ✖ What is the molar flowrate of flue gas if its molar mass is 28.27 g/mole?
 - + 5875 kg/h / (28.27 kg/kmole) = 207.82 kmole / h
- ✖ Check the ppm concentration of m-xylene?
 - + 0.291 kmole/h / 207.82 kmole/h = 0.0014 kmole/kmole = 1400 ppm

EXAMPLE

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- ✖ Check if the industry meets emission standard?
 - + 7975 mg/Nm³ > 500 mg/Nm³ → Fails