

**YILDIZ TECHNICAL UNIVERSITY**  
**CIVIL ENGINEERING DEPARTMENT CONSTRUCTION MATERIALS DIVISION**  
**MATERIALS SCIENCE AND ENGINEERING/ PRACTICE 1**

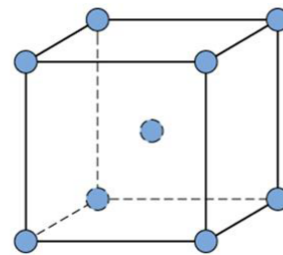
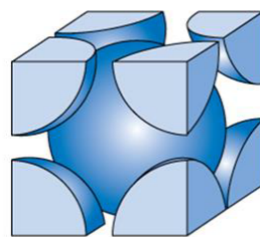
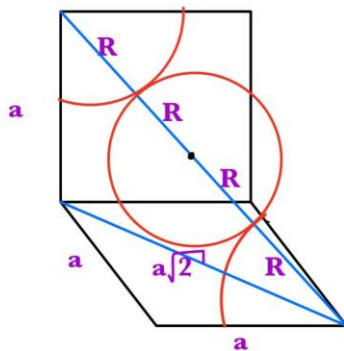
**QUESTION 1**

A material has a body-centered cubic (BCC) crystal structure with an atomic radius ( $r$ ) of 1.857 Å and atomic mass of 23 g/mol. According to this:

a) Find the length of the unit cell ( $a$ ), the specific gravity ( $\gamma$ ), the atomic packing factor (APF).

Solution 1:

The body-centered cubic (BCC) crystal structure contains nine atoms: one on each corner of the cube and one atom in the center. Because the volume of each corner atom is shared between adjacent cells, **each BCC cell contains two atoms.**



Total number of atoms in the unit cell:

$$n = 1/8 * 8 + 1 = 2 \text{ atoms}$$

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$$\text{a) } (4R)^2 = a^2 + (a\sqrt{2})^2 \quad \frac{a=4R}{\sqrt{3}} \quad a_{KHM} = \frac{4R}{\sqrt{3}} = \frac{4 \cdot (1,857 \text{ Å})}{\sqrt{3}} = 4,29 \text{ Å}$$

Since the entire crystal can be generated by the repetition of the unit cell, the theoretical density of a crystalline material can be calculated based on the density of the unit cell:

$$\rho = \frac{nA}{V_c N_A}$$

$\rho$  : Density

$n$  : Number of atoms in each unit cell

$A$  : Atomic weight (g/mol)

$V_c$  : Volume of the unit cell

$N_A$  : Avogadro's number

$$N_A = (0.602 \times 10^{24} \text{ atoms/mol})$$

$$n = 8(1/8) + 1 = 2 \text{ atom}$$

$$V = (a)^3 = (4R/\sqrt{3})^3$$

$$\rho = \frac{2}{(4R/\sqrt{3})^3} \cdot \frac{23}{0.602 \times 10^{24}} = 0.968 \text{ gr / cm}^3$$

$1.857 \times 10^{-8}$

Atomic packing factor shows us how dense the unit cell is:

$$APF = \frac{\text{Volume of atoms in a unit cell}}{\text{Total unit cell volume}}$$

$$APF = \frac{2 \times \frac{4}{3} \pi R^3}{a^3} = \frac{2 \times \frac{4}{3} \pi (1.857 \times 10^{-8})^3}{(4.29 \times 10^{-8})^3} = 0.68$$

## **QUESTION 2**

A 10 cm cube made of a stone with a unit weight of  $2.34 \text{ g/cm}^3$  and a specific gravity of  $2.72 \text{ g/cm}^3$ , weighs 2445 g when it is saturated.

- a) Calculate compactness (k) and porosity (p).
- b) Calculate water absorption ratio by mass ( $a_m$ ) and by volume ( $a_v$ ).
- c) The same material absorbs 25.2 g water from its base for 64<sup>th</sup> minutes by capillarity. According to this, calculate the time that water rises up to the top surface of a structural element with height of 3 m.

### **Solution 2:**

#### **a) Unit Weight (Density) ( $\beta$ )**

Density ( $\beta$ ) is defined as the dry weight ( $W_o$ ) of a given volume ( $V_t$ ) of a material. Density has a strong relation with strength and thermal conductivity.

$$\beta = \frac{W_o}{V_t}$$

#### **b) Specific gravity ( $\gamma$ )**

Specific gravity ( $\gamma$ ) is the dry weight ( $W_o$ ) of a given volume of the solid phase ( $V_s$ ) of a material.

$$\gamma = \frac{W_o}{V_s}$$

#### **c) Compactness ratio (k)**

The ratio of solid volume of a material ( $V_s$ ) to its total volume ( $V_t$ ) and can also be calculated by dividing density ( $\beta$ ) by specific gravity ( $\gamma$ ).

$$k = \frac{V_s}{V_t} = \frac{\beta}{\gamma}$$

#### **d) Porosity (p)**

The ratio of the pore volume ( $V_p$ ) to the total volume ( $V_t$ ) of the material. Porosity (p) defines total pores, whereas effective porosity ( $p_e$ ) defines open, interconnected and continuous pores.

$$p = \frac{V_p}{V_t} = 1 - k$$

$$\beta = 2,34 \text{ g} / \text{cm}^3$$

$$\gamma = 2,72 \text{ g} / \text{cm}^3$$

$$k = \frac{\beta}{\gamma} = \frac{2,34}{2,72} = 0.86 = \%86$$

$$p = 1 - k = 1 - 0,86 = 0.14 = \%14$$

**e) Water absorption by mass ( $a_m$ ):** The ratio of the increase in mass to the mass of the dry sample.

$$a_m = \frac{W_{SSD} - W_o}{W_o}$$

SSD: **S**aturated and **S**urface **D**ry

$W_{SSD}$ : The weight of the sample in the SSD state

$W_o$ : The weight of the sample in dry state

**f) Water absorption by volume ( $a_v$ ):** The ratio of the increase in volume to the total volume.

$$a_v = \frac{(W_{SSD} - W_o) / \rho_{water}}{V_t}$$

$\rho_{water} \approx 1 \text{ g/cm}^3$

$$a_v = \beta \cdot a_m$$

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$$\beta = 2.34 = \frac{W_0}{V_T} = \frac{W_0}{10 \times 10 \times 10} \implies W_0 = 2340 \text{ g}$$

$$a_m = \frac{2445 - 2340}{2340} = \%4.5$$

$$a_v = \frac{2445 - 2340}{10 \times 10 \times 10} = \%10.5$$

**Capillarity** can be defined as the tendency of a water in a capillary pores of a material to rise as a result of surface tension.

**g) Capillary Water Absorption Coefficient (K, cm<sup>2</sup>/s)**

Defined as the "absorbed water amount (Q) from unit surface area (A) of a material in unit time (t)".

$$K_i = \frac{Q_i^2}{A^2 t_i}$$

$$Q_i = 25.2g$$

$$t = 64 \text{ min}$$

$$K_i = \frac{(25.2)^2}{(10 \times 10)^2 \times (64 \times 60)} = 0,0000165 \text{ cm}^2 / s$$

$$t = \frac{Q_{\max}^2}{A^2 \cdot K} \implies Q_{\max} = a_v \times V = (10 \times 10 \times 300) \times (0.105) = 3150 \text{ cm}^3$$

$$t = \frac{(3150)^2}{(10 \times 10)^2 \times 0,0000165} = 60136363,645 \text{ sn} = 696 \text{ days} = 23,2 \text{ months}$$

### QUESTION 3

The capillarity experiment was performed on a stone sample with the dimensions of 10x10x10 cm and the results are given below:

|                |     |     |     |     |     |     |     |
|----------------|-----|-----|-----|-----|-----|-----|-----|
| <b>t (min)</b> | 0   | 1   | 4   | 9   | 16  | 25  | 36  |
| <b>W (g)</b>   | 620 | 622 | 624 | 627 | 629 | 631 | 632 |

a) According to the given data, draw the “absorbed water amount (Q, cm<sup>3</sup>) – time (t, minute)” graphic of this material.

b) Calculate the capillarity coefficient of this material by considering amount of absorbed water at 36<sup>th</sup> minutes.

Solution 3:

$$Q_n = W_n - W_0$$

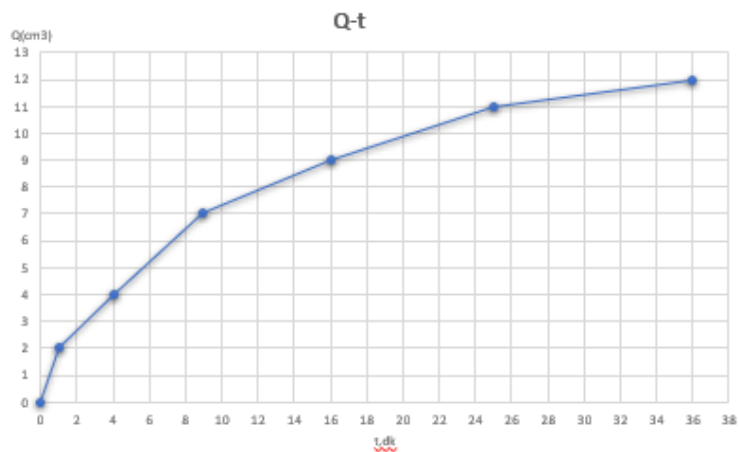
$$Q_1 = W_1 - W_0$$

$$Q_2 = W_2 - W_0$$

$$Q_1 = 622 - 620 = 2 \text{ gr}$$

$$Q_2 = 624 - 620 = 4 \text{ gr}$$

$$Q_9 = 627 - 620 = 7 \text{ gr}$$



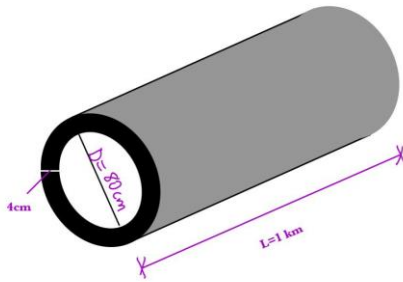
$$K = \frac{Q^2}{A^2 \cdot t} = \frac{(632 - 620)^2}{(10 \times 10)^2 \times 36 \times 60} = 6,7 \times 10^{-6} \text{ cm}^2 / \text{sn}$$

#### QUESTION 4

A concrete pipe has internal diameter of 80 cm and wall thickness of 4 cm. Permeability coefficient ( $K_p$ ) of the concrete is  $2 \times 10^{-8}$  cm/sec. Calculate the amount of water loss daily under 6 atm pressure for a length of 1 km?

Note: 1 atm  $\approx$  1000 cm-water column

Solution 4:



### 4.6. Permeability

Water permeability of a material is expressed by the coefficient of water permeability ( $K_p$ , cm/sec), which is measured by determining the rate of water flow through the material **under pressure**.

$$K_p = \frac{Qxh}{PxAct}$$

In the equation,

$Q$  is the amount of water that flows through the sample ( $\text{cm}^3$ ),

$h$  is the thickness of the sample that water flows through (cm),

$P$  is the pressure in

$A$  is the cross-section of the sample ( $\text{cm}^2$ ) and  $t$  is time in seconds.

$$P = 6 \text{ atm} = 6000 \text{ cm-hydraulic column (water-column),}$$

$$A = 2 \cdot \pi \cdot r \cdot L = \pi \cdot 80 \cdot 10^5 = 25120000 \text{ cm}^2$$

$$Q = \frac{\Delta P \cdot A \cdot t}{h} \cdot k_p = \frac{2 \times 10^{-9} \times 6000 \times 86400 \times 25120000}{4} :$$

$$= 6511104 \text{ cm}^3 = 6,511 \text{ m}^3$$

## **QUESTION 5**

A S420 class steel sample with a nominal diameter of 16 mm ( $\phi 16$ ) was subjected to the uniaxial tension test. The gauge length of the extensometer ( $l_0$ ) is 100 mm and the results are given below:

|                               |   |       |       |       |       |       |        |        |          |
|-------------------------------|---|-------|-------|-------|-------|-------|--------|--------|----------|
| P (Load, N)                   | 0 | 20100 | 40200 | 60300 | 80400 | 88400 | 108500 | 124600 | 115600   |
| $\Delta l$ (Displacement, mm) | 0 | 0.045 | 0.090 | 0.135 | 0.180 | 0.280 | 6.30   | 9.20   | Fracture |

According to the given data:

- Draw the stress-strain ( $\sigma$ - $\epsilon$ ) curve and calculate the limit of proportionality ( $\sigma_p$ ), the yield strength ( $\sigma_y$ ), the tensile strength ( $\sigma_t$ ).
- Calculate the modulus of elasticity (E)
- Calculate the ductility ( $\epsilon_k$ ) if the final gauge length is measured as 90.0 mm after the fracture.
- Calculate the resilience ( $W_R$ ) and the toughness ( $W_T$ ) of this specimen.

Solution 5:

Stress and strain data points can be determined by using load and deformation measurements

$$d_0 = 16 \text{ mm}$$

$$l_0 = 10 \text{ cm} = 100 \text{ mm}$$

$$A_0 = \frac{\pi \times d_0^2}{4} = \frac{\pi \cdot 16^2}{4} = 201 \text{ mm}^2 \quad (201 \text{ mm}^2)$$

$$\sigma_i = \frac{P_i}{A_0}$$

$$\epsilon_i = \frac{l - l_0}{l_0} = \frac{\Delta l}{l_0}$$

$$\sigma_1 = 20100 / 201 = 100 \text{ N/mm}^2 = 100 \text{ MPa}$$

$$\sigma_2 = 40200 / 201 = 200 \text{ MPa}$$

$$\sigma_3 = 60300 / 201 = 300 \text{ MPa}$$

$$\sigma_4 = 80400 / 201 = 400 \text{ MPa}$$

$$\sigma_5 = 88400 / 201 = 440 \text{ MPa}$$

$$\sigma_6 = 108500 / 201 = 540 \text{ MPa}$$

$$\sigma_7 = 124600 / 201 = 620 \text{ MPa}$$

$$\epsilon_1 = 0,045 / 100 = 4,5 \times 10^{-4}$$

$$\epsilon_2 = 0,090 / 100 = 9,0 \times 10^{-4}$$

$$\epsilon_3 = 0,135 / 100 = 13,5 \times 10^{-4}$$

$$\epsilon_4 = 0,180 / 100 = 18,0 \times 10^{-4}$$

$$\epsilon_5 = 0,280 / 100 = 28,0 \times 10^{-4}$$

$$\epsilon_6 = 6,300 / 100 = 630 \times 10^{-4}$$

$$\epsilon_7 = 9,200 / 100 = 920 \times 10^{-4}$$

$$\sigma_8 = 115600 / 201 = 575 \text{ MPa}$$



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- **PL: Proportional limit ( $\sigma_p$ )**

In the stress level up to PL (i.e., the linear elastic limit), Hooke's law is obeyed.

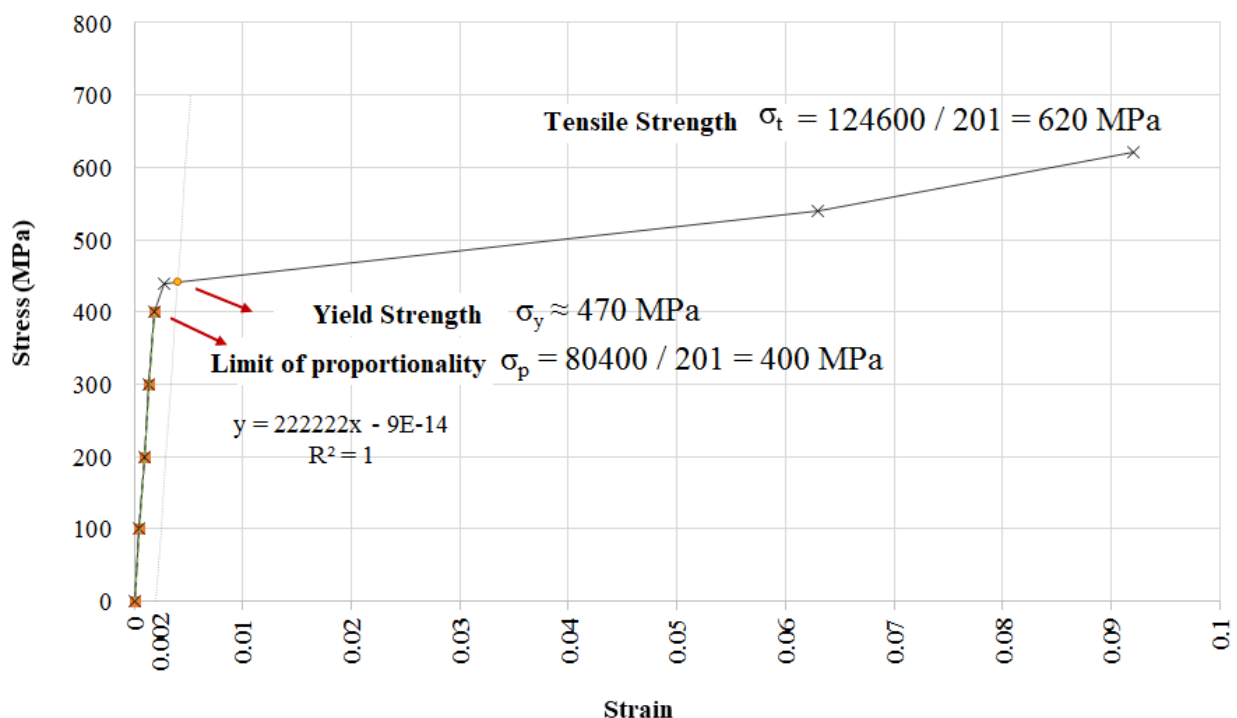
- **YS: Yield Strength ( $\sigma_y$ )**

For engineering applications, it is desirable to know the stress level at which plastic deformation begins, or where the phenomenon of **yielding** occurs. For metals that experience

- **TS: Tensile Strength ( $\sigma_t$ )**

When stress continues in the plastic regime, the stress-strain passes through a maximum (*point M*), called the tensile strength, and then falls as the material starts to develop a neck and it finally breaks at the fracture point (*F*).

$$\sigma_t = \frac{P_{\max}}{A_o}$$



The slope of this linear segment corresponds to the modulus of elasticity (E).

This modulus may be thought of as stiffness, or a material's resistance to elastic deformation.

### Çözüm b)

$$E = \Sigma \sigma_i \cdot \epsilon_i / \Sigma \epsilon_i^2$$

| $\sigma_i$ (MPa) | $\epsilon_i$          | $\sigma_i \times \epsilon_i$ (MPa) | $\epsilon_i^2$                  |
|------------------|-----------------------|------------------------------------|---------------------------------|
| 0                | 0                     | 0                                  | 0                               |
| 100              | $4,5 \times 10^{-4}$  | 0,045                              | $20,2 \times 10^{-8}$           |
| 200              | $9,0 \times 10^{-4}$  | 0,180                              | $81,3 \times 10^{-8}$           |
| 300              | $13,5 \times 10^{-4}$ | 0,405                              | $182 \times 10^{-8}$            |
| 400              | $18 \times 10^{-4}$   | 0,720                              | $324 \times 10^{-8}$            |
| 440              | $28 \times 10^{-4}$   | $\Sigma = 1,35$                    | $\Sigma = 607,5 \times 10^{-8}$ |
| 540              | $630 \times 10^{-4}$  |                                    |                                 |
| 620              | $920 \times 10^{-4}$  |                                    |                                 |
| 575              | —                     |                                    |                                 |

#### Elastisite Modülü

$$E = \Sigma \sigma_i \cdot \epsilon_i / \Sigma \epsilon_i^2$$

$$E = 1,35 / (607,5 \times 10^{-8}) = 222222 \text{ MPa} = 222,2 \text{ GPa}$$

c) Calculate the ductility ( $\epsilon_k$ ) if the final gauge length is measured as 90.0 mm after the fracture.

#### • D: Ductility (% $\epsilon_f$ ):

Ductility may be expressed quantitatively as either percent elongation (% $\epsilon_f$ ) or percent reduction in area (% $R_A$ ). The percent elongation % $\epsilon_f$  is the percentage of plastic strain at fracture point:

$$\% \epsilon_f = \frac{l_f - l_i}{l_i} \times 100$$

$$l_i = 5 \times d_o = 5 \times 16 = 80 \text{ mm}$$

$$l_{\text{final}} = 90 \text{ mm}$$

$$\epsilon_f = (90 - 80) / 80 = 0,125 = \%12,5$$

## Resilience

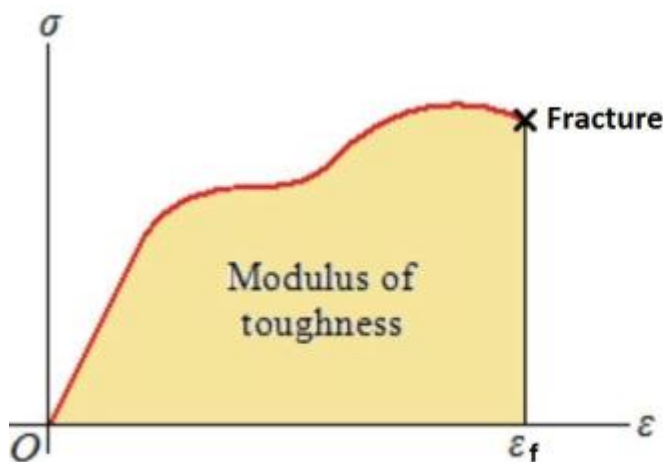
Resilience is the capacity of a material to absorb energy when it is deformed elastically.

$$W_R = \frac{\sigma_y \times \varepsilon_y}{2} = \frac{\sigma_y}{2} \times \frac{\sigma_y}{E} = \frac{\sigma_y^2}{2E} = \frac{470^2}{2 \times 222222} = 0,50 MPa$$

## Toughness

Toughness is a measure of the ability of a material to absorb energy up to fracture.

Modulus of toughness ( $W_T$ ) is the area under the stress-strain curve up to the fracture point. In other words, toughness is the energy per unit volume is the total area under the strain-stress curve.



$$W_T = \int_0^{\varepsilon_f} \sigma d\varepsilon$$

- Assuming a right trapezoid:

$$W_T = \frac{\sigma_y + \sigma_t}{2} \times \varepsilon_f$$

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$$W_T = \frac{(\sigma_y + \sigma_t)}{2} \times \varepsilon_f = \frac{470 + 620}{2} \times 0,125 = 68,13 MPa$$

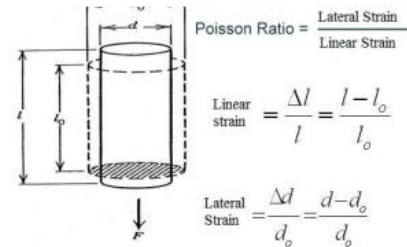
### QUESTION 6

A tensile stress is to be applied along the long axis of a cylindrical brass rod that has a diameter of 10 mm. Determine the magnitude of the load required to produce a  $2.5 \cdot 10^{-3}$  mm change in diameter if the deformation is entirely elastic. (For brass, the modulus of elasticity is 97 GPa and the Poisson's ratio is 0.34).

Solution 6:

- A parameter termed Poisson's ratio ( $\nu$ ) is defined as the ratio of the lateral and axial strains:

$$\nu = - \frac{\epsilon_{lateral}}{\epsilon_{axial}}$$



The negative sign is included in the expression so that ( $\nu$ ) will always be positive, since ( $\epsilon_{lateral}$ ) and ( $\epsilon_{axial}$ ) will always be of opposite sign.

$$0.34 = - \frac{\xi_{lateral}}{\xi_{axial}} \implies \xi_{lateral} = \frac{\Delta l}{l} = \frac{2.5 \times 10^{-3}}{10} = 2.5 \times 10^{-4}$$

$$0.34 = \frac{2.5 \times 10^{-4}}{\xi_{axial}} \implies \xi_{axial} = 7.35 \times 10^{-4}$$

$$\sigma = E \epsilon$$

$$\sigma = 97000 \times 7.35 \times 10^{-4} = 71.323 \text{ Mpa}$$

$$\sigma = 71.323 = \frac{P}{A} = \frac{P}{\pi \times 10^2 / 4}$$

$$P = 5598.9 \text{ N}$$