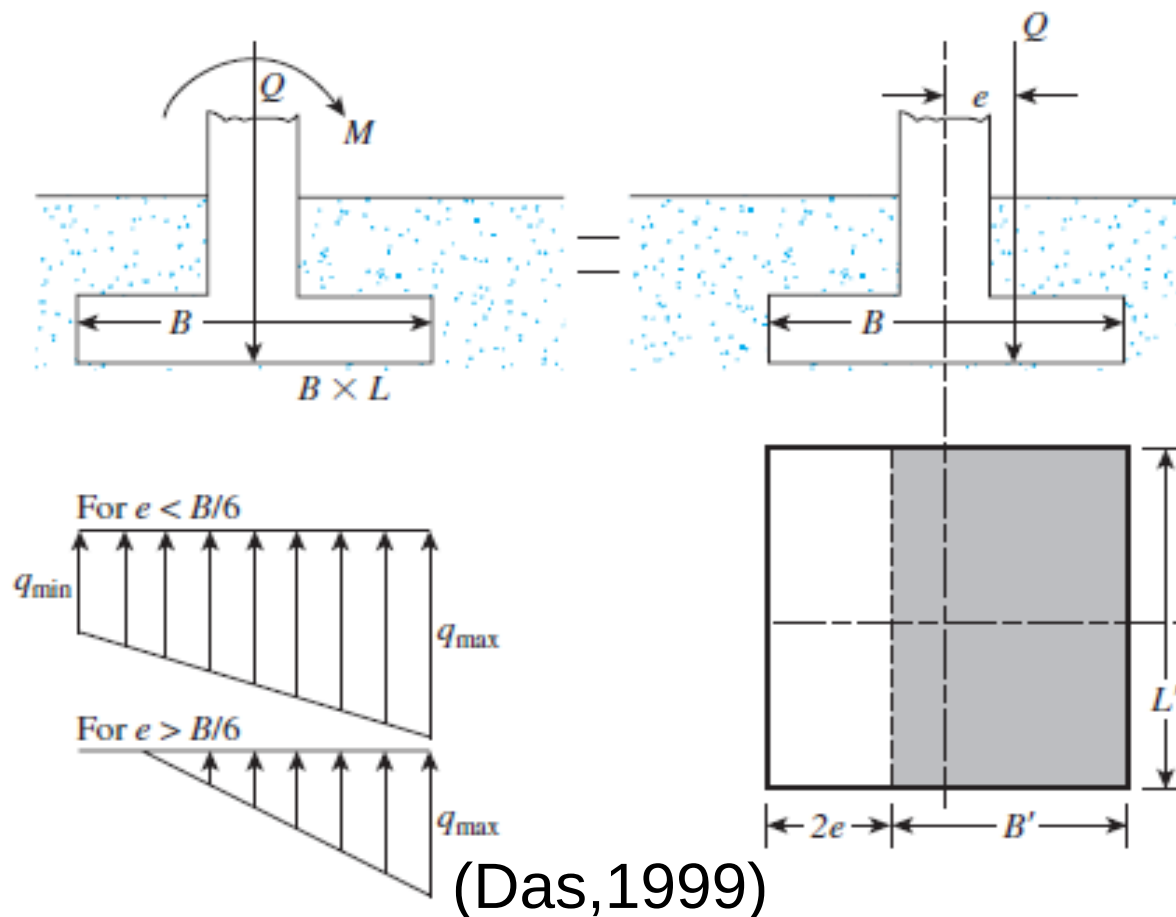


Eccentricity

$$q_{\max} = \frac{Q}{BL} + \frac{6M}{B^2L}$$

$$q_{\min} = \frac{Q}{BL} - \frac{6M}{B^2L}$$



one-way eccentricity

$$\acute{A} = \acute{B} \acute{L} \quad (\text{the base area of foundation})$$

$$\acute{B} = B - 2e$$

$$\acute{L} = L$$

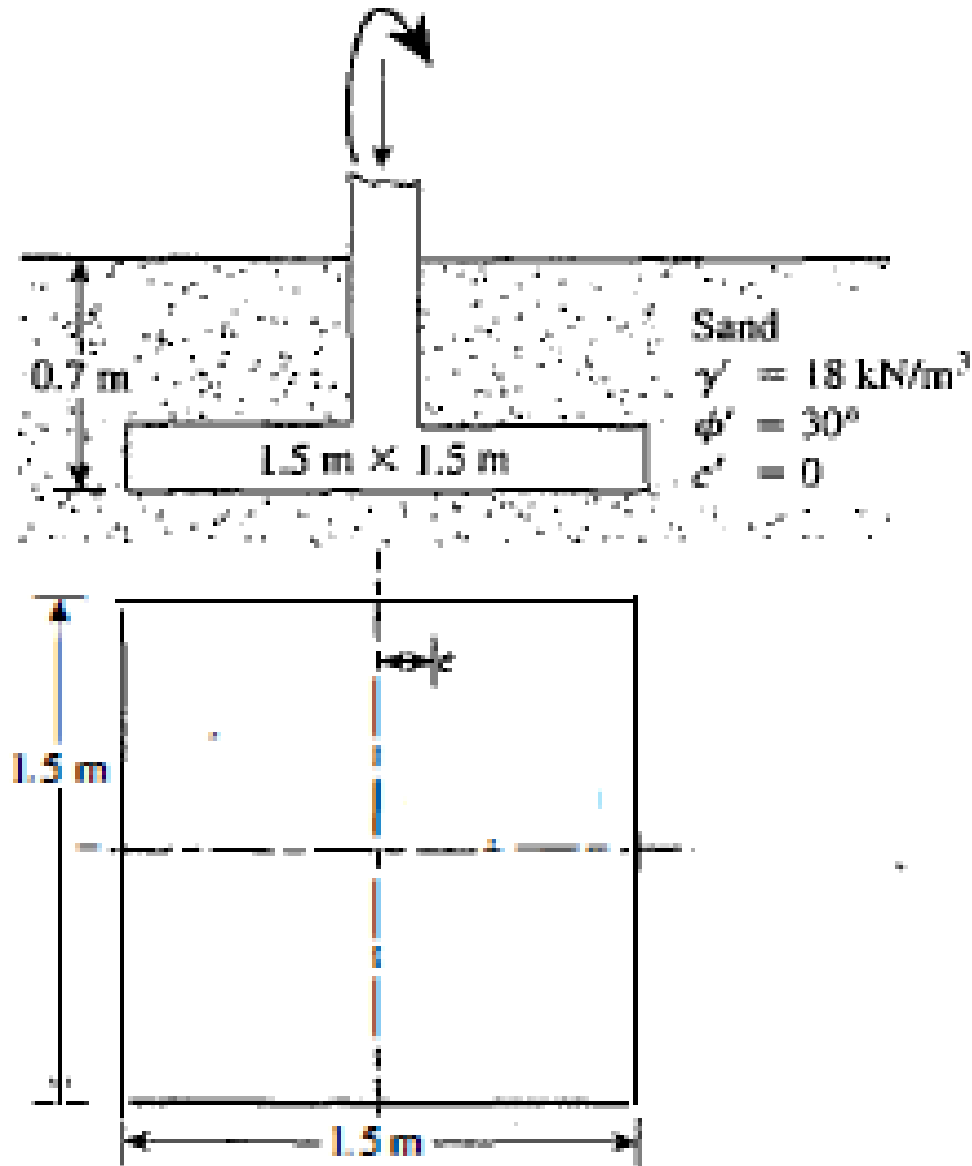
$$q_{ult} = cN_c s_c d_c i_c g_c b_c + qN_q s_q d_q i_q g_q b_q + \frac{1}{2} \acute{B} \gamma N_\gamma s_\gamma d_\gamma i_\gamma g_\gamma b_\gamma$$

$$Q_{ult} = q_{ult} \acute{A}$$

$$q_a = \frac{q_{ult}}{\text{factor of safety}} = \frac{Q_a}{\acute{B} \acute{L}}$$

$$Q_a = q_a \acute{A} = q_a \acute{B} \acute{L}$$

$$e_B = 0.15, Q_{ult} = ?$$



(Das, 1999)

$$q = (0.7)(18) = 12.6kPa$$

$$\acute{B} = 1.5 - 2(0.15) = 1.2m \quad \acute{L} = L = 1.5m$$

$$s_q = 1 + \left(\frac{\acute{B}}{\acute{L}} \tan \phi\right) = 1 + \frac{1.2m}{1.5m} \tan 30^\circ = 1.462$$

$$d_q = 1 + \left[2 \tan \phi (1 - \sin \phi)^2 \frac{D_f}{B}\right] = 1 + \left[2 \tan 30 (1 - \sin 30)^2 \frac{0.7m}{1.5m}\right] = 1.135$$

$$s_\gamma = 1 - 0.4 \left(\frac{\acute{B}}{\acute{L}}\right) = 1 - 0.4 \frac{1.2m}{1.5m} = 0.68 \quad d_\gamma = 1$$

$$\begin{aligned} q_{ult} &= q N_q s_q d_q + \frac{1}{2} \acute{B} \gamma N_\gamma s_\gamma d_\gamma = 549kPa \\ &= (12.6)(18.4)(1.462)(1.135) \\ &\quad + (0.5)(18 \frac{kN}{m^3})(1.2m)(22.4)(0.68)(1) \end{aligned}$$

$$Q_{ult} = q_{ult} \dot{A} = 549kPa(1.2m)(1.5m) = 988kN$$

Two-way eccentricity

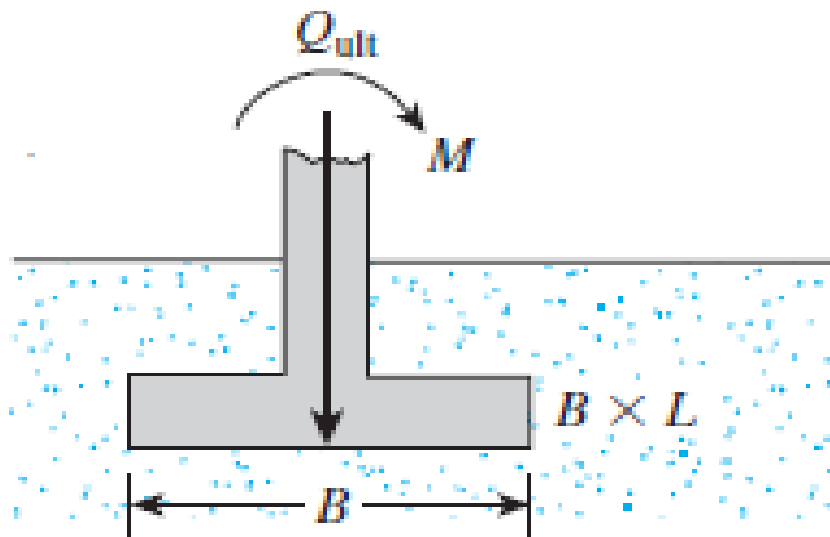
$$\acute{A} = \acute{B}x\acute{L} \quad (\text{the base area of foundation})$$

$$q_{ult} = cN_c s_c d_c i_c g_c b_c + qN_q s_q d_q i_q g_q b_q + \frac{1}{2} \acute{B} \gamma N_\gamma s_\gamma d_\gamma i_\gamma g_\gamma b_\gamma$$

$$Q_{ult} = q_{ult} \acute{A}$$

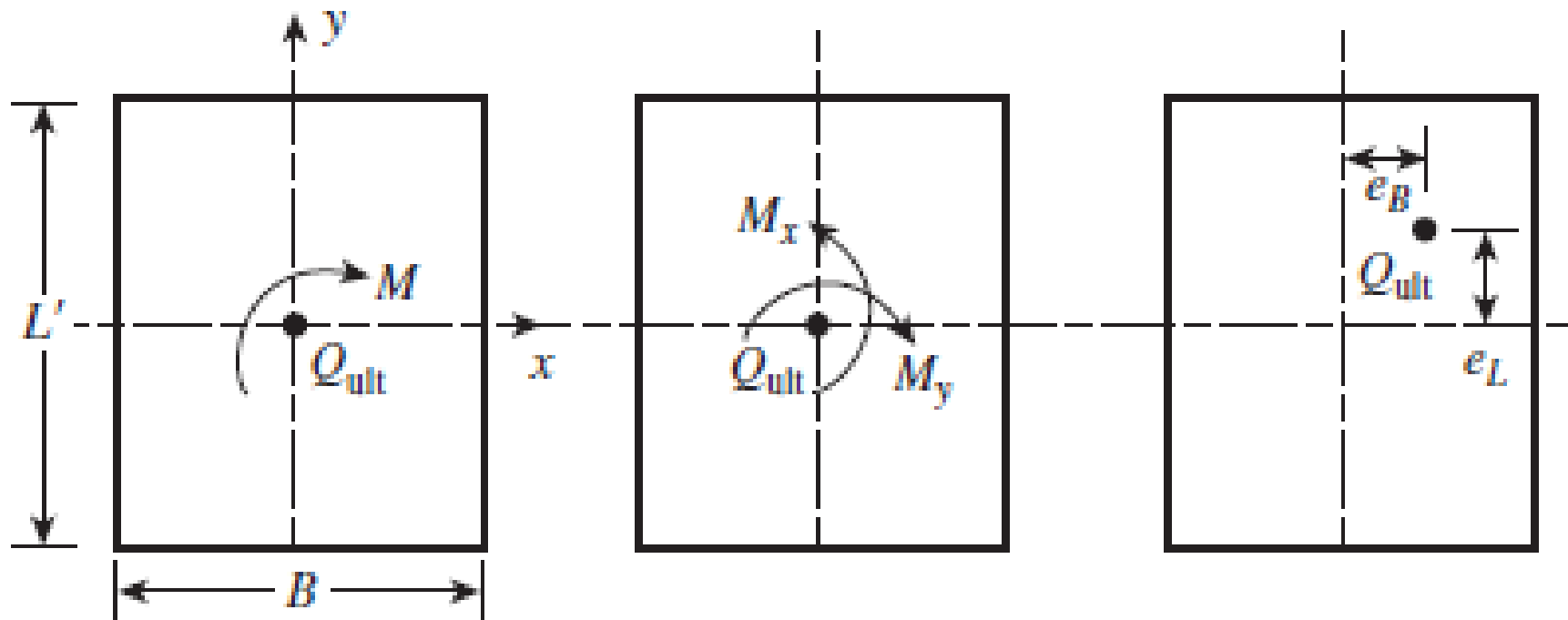
$$q_a = \frac{q_{ult}}{\text{factor of safety}} = \frac{Q_a}{\acute{B}x\acute{L}}$$

$$Q_a = q_a \acute{A} = q_a \acute{B} \acute{L}$$



$A' = \text{effective area} = B' L'$

$$Q_{ult} = q_{ult} \dot{A} = q_{ult} \dot{B} \dot{L}$$



(Das, 1999)

Case 1. $e_L/L \geq \frac{1}{6}$ and $e_B/B \geq \frac{1}{6}$.

$$A' = \frac{1}{2}B_1L_1$$

where

$$B_1 = B \left(1.5 - \frac{3e_B}{B} \right)$$

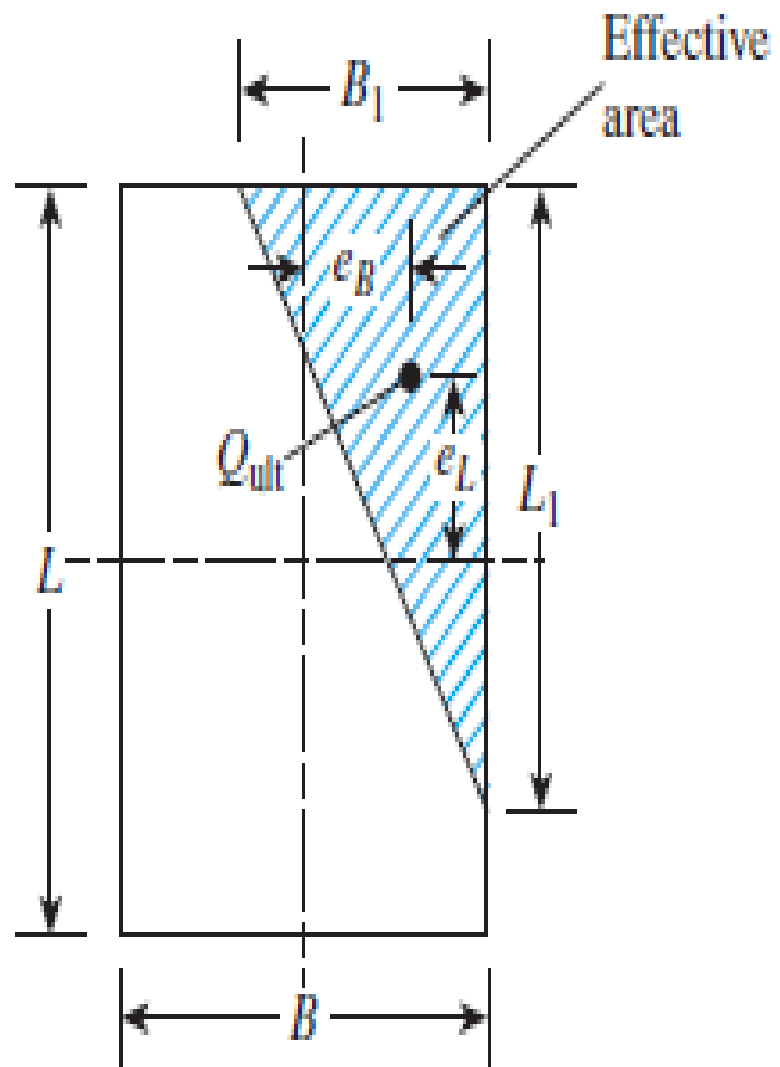
and

$$L_1 = L \left(1.5 - \frac{3e_L}{L} \right)$$

The effective length L' is the larger of the two dimensions B_1 and L_1 . So the effective width is

$$B' = \frac{A'}{L'}$$

(Das,1999)



Effective area for the case of $e_L/L \geq \frac{1}{6}$
 and $e_B/B \geq \frac{1}{6}$

(Das, 1999)

Case II. $e_L/L < 0.5$ and $0 < e_B/B < \frac{1}{6}$.

$$A' = \frac{1}{2}(L_1 + L_2)B$$

The effective length is

$$L' = L_1 \text{ or } L_2 \quad (\text{whichever is larger})$$

$$B' = \frac{A'}{L_1 \text{ or } L_2 \quad (\text{whichever is larger})}$$

The effective length is

$$L' = L_1 \text{ or } L_2 \quad (\text{whichever is larger})$$

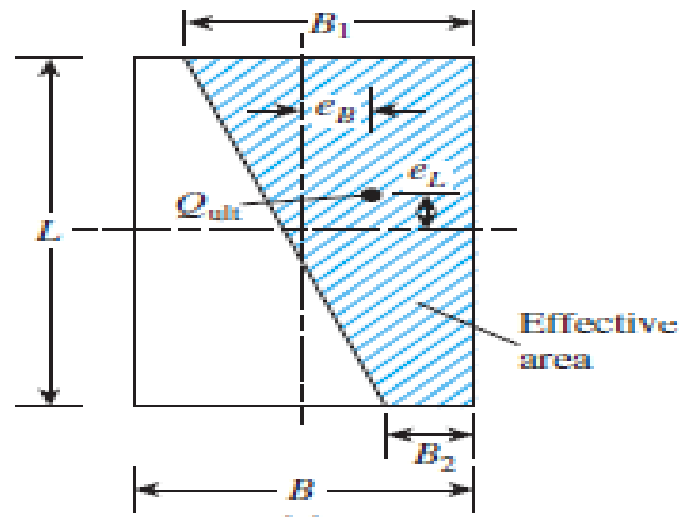
(Das,1999)

Case III. $e_L/L < \frac{1}{6}$ and $0 < e_B/B < 0.5$.

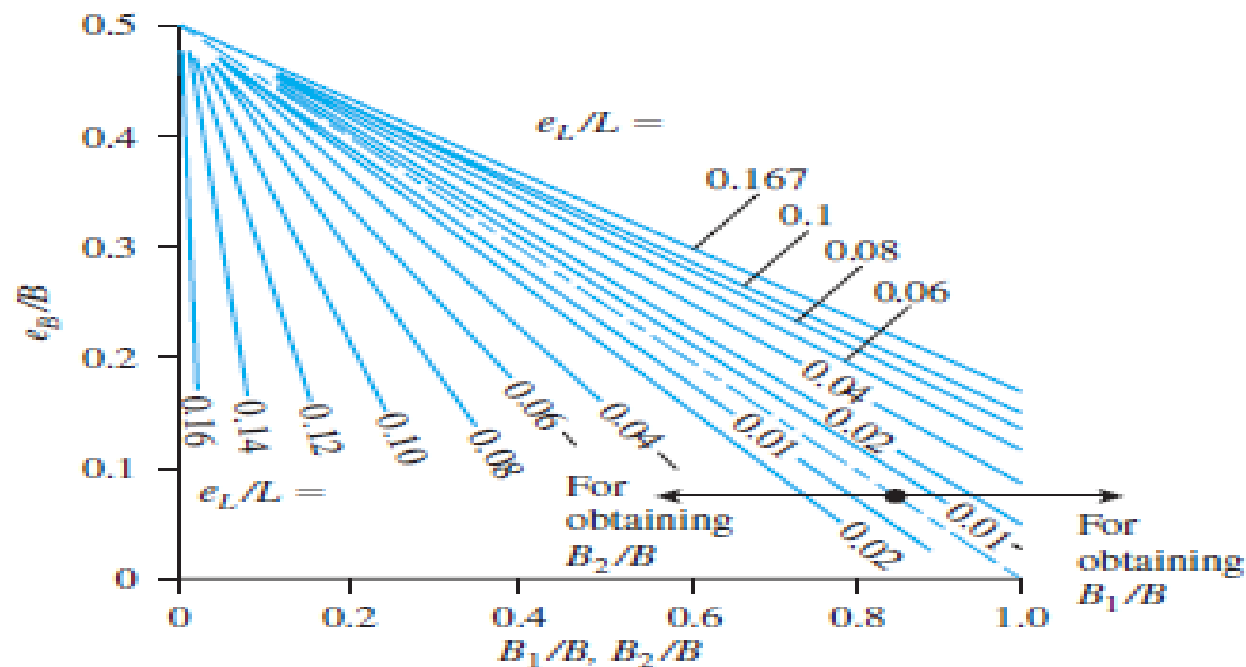
$$A' = \frac{1}{2}(B_1 + B_2)L$$

$$L' = L$$

$$B' = \frac{A'}{L}$$



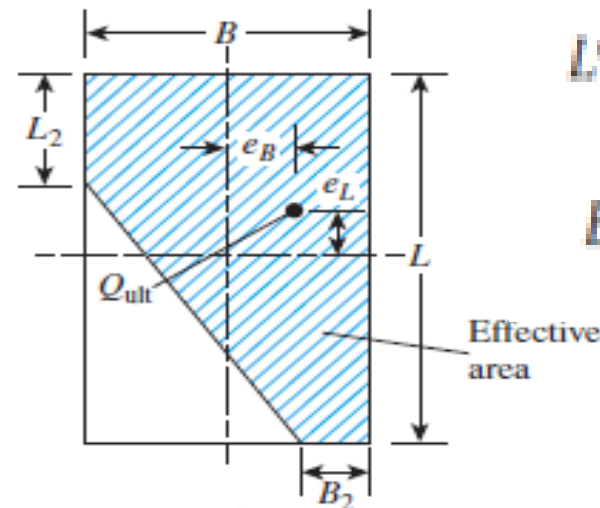
(Das,1999)



Effective area for the case of $e_L/L < \frac{1}{6}$ and $0 < e_B/B < 0.5$ (After Hightner and Anders, 1985) Hightner, W. H. and Anders, J. C. (1985). "Dimensioning Footings Subjected to Eccentric Loads," *Journal of Geotechnical Engineering*, American Society of Civil Engineers, Vol. 111, No. GT5, pp. 659–665. With permission from ASCE.)

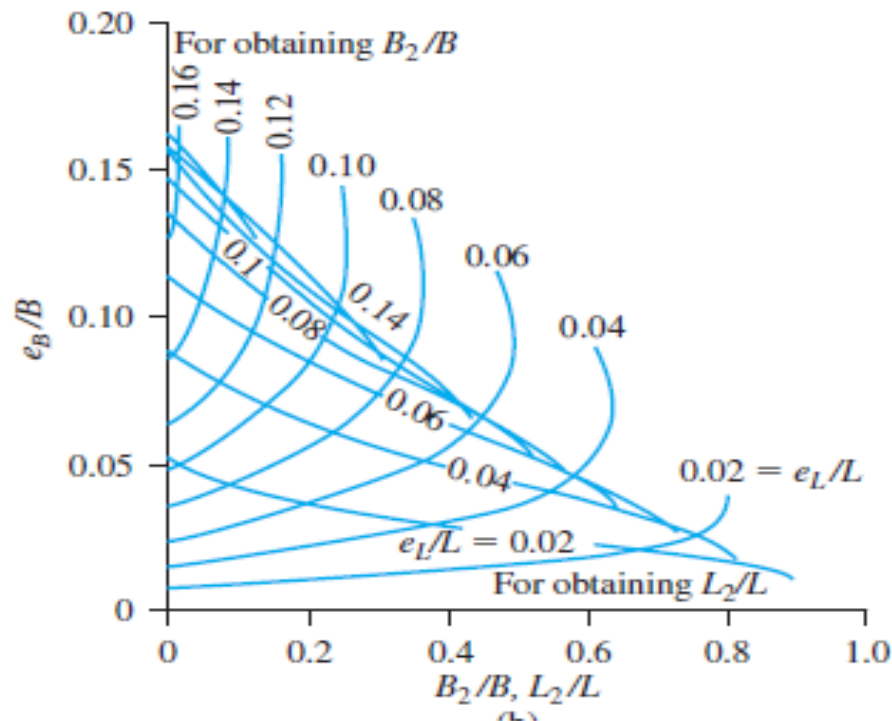
Case IV. $e_L/L < \frac{1}{6}$ and $e_B/B < \frac{1}{6}$.

$$A' = L_2 B + \frac{1}{2}(B + B_2)(L - L_2)$$



$$L' = L$$

$$B' = \frac{A'}{L}$$

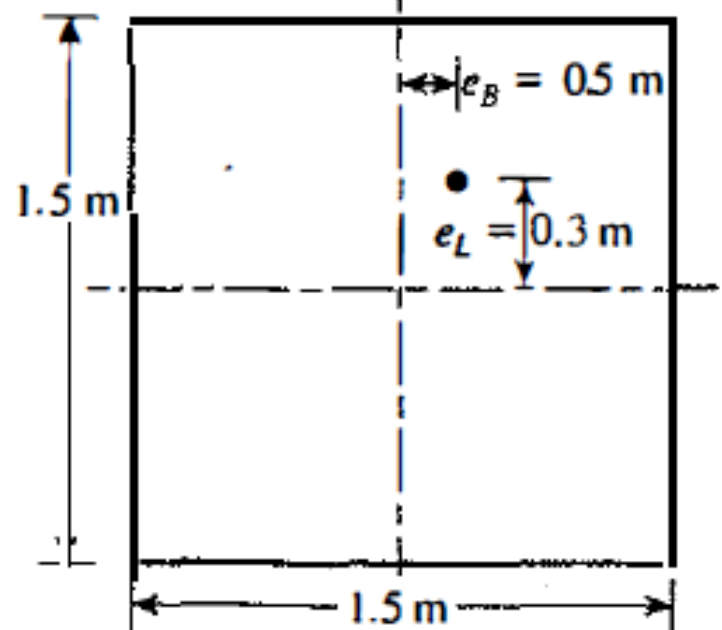
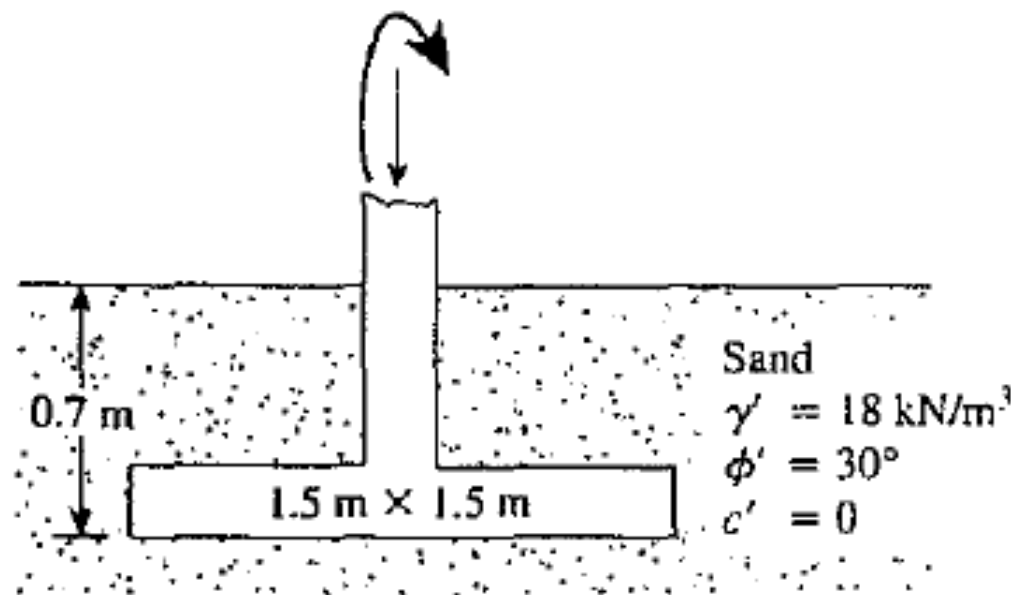


Effective area for the case of $e_L/L < \frac{1}{6}$ and $e_B/B < \frac{1}{6}$ (After Hightner and Anders, 1985) (Hightner, W. H. and Anders, J. C. (1985). "Dimensioning Footings Subjected to Eccentric Loads," *Journal of Geotechnical Engineering*, American Society of Civil Engineers, Vol. 111, No. GT5, pp. 659–665. With permission from ASCE.)

(Das,1999)

$$e_B = 0.15 \text{ and } e_L = 0.3; \text{ } Q_{ult} = ?$$

There is a two way-eccentricity



$$\frac{e_L}{L} = \frac{0.3}{1.5} = 0.2$$

$$\frac{e_B}{B} = \frac{0.15}{1.5} = 0.1$$

Case II

$$\frac{L_1}{L} \approx 0.85; \quad L_1 = (0.85)(1.5) = 1.275 \text{ m} \quad \frac{L_2}{L} \approx 0.21; \quad L_2 = (0.21)(1.5) = 0.315 \text{ m}$$

(Das, 1999)

$$A' = \frac{1}{2}(L_1 + L_2)B = \frac{1}{2}(1.275 + 0.315)(1.5) = 1.193 \text{ m}^2$$

$$L' = L_1 = 1.275 \text{ m} \quad B' = \frac{A'}{L'} = \frac{1.193}{1.275} = 0.936 \text{ m}$$

$$s_c = 1.0 + \frac{N_q}{N_c} \cdot \frac{B}{L}$$

$$s_q = 1.0 + \frac{B}{L} \tan \phi = 1 + \left(\frac{B'}{L'} \right) \tan \phi' = 1 + \left(\frac{0.936}{1.275} \right) \tan 30^\circ = 1.424$$

$$s_\gamma = 1.0 - 0.4 \frac{B}{L} = 1 - 0.4 \left(\frac{B'}{L'} \right) = 1 - 0.4 \left(\frac{0.936}{1.275} \right) = 0.706$$

$$d_q = 1 + 2 \tan \phi (1 - \sin \phi)^2 k = 1 + 2 \tan \phi' (1 - \sin \phi') \cdot \frac{D_f}{B} = 1 + \frac{(0.289)(0.7)}{1.5}$$

$$d_\gamma = 1.00$$

$$\phi = 30^\circ \Rightarrow N_c = 30.13; \quad N_q = 18.4; \quad N_\gamma = 22.4$$

(Das,1999)

$$q_{ult} = cN_c s_c d_c + qN_q s_q d_q + \frac{1}{\gamma} \dot{B} \gamma N_\gamma s_\gamma d_\gamma$$

$$q_{ult} = 0 + (0.7 \times 18)(18.4)(1.424)(1.135) + \frac{1}{2}(0.936)(18)(22.4)$$

$$Q_{ult} = q_{ult} \dot{A} = q_{ult} \dot{B} L' = q_{ult}(0.936 \times 1.275) = 600 \text{ kN}$$

(Das, 1999)